

VISUALIZING MULTI-ATTRIBUTE DATA

DATA TABLES

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RECAP

you have learned about

- visual variables and marks
- that their perceptual properties matter

RECAP

➔ Magnitude Channels: Ordered Attributes

Position on common scale 

Position on unaligned scale 

Length (1D size) 

Tilt/angle 

Area (2D size) 

Depth (3D position) 

Color luminance 

Color saturation 

Curvature 

Volume (3D size) 

▲ Most
Effectiveness
Least ▼

➔ Identity Channels: Categorical Attributes

Spatial region 

Color hue 

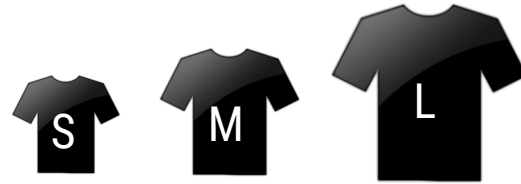
Motion 

Shape 

RECAP

DATA TYPES

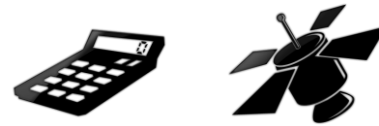
ORDINAL (ranking)



NOMINAL (categorical)

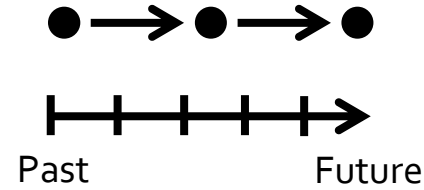


QUANTITATIVE (numerical)

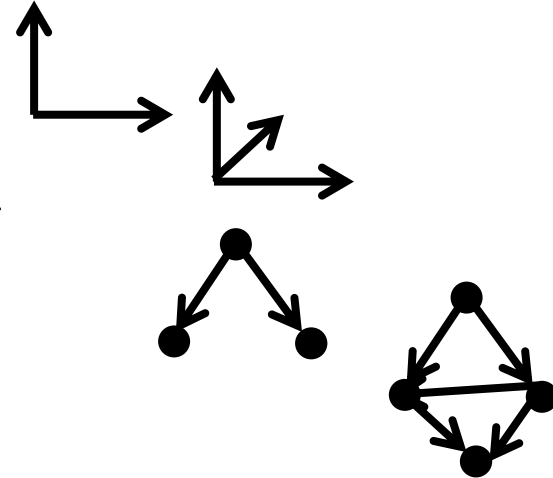


RECAP

- 1D (linear)
- Temporal
- 2D (maps)
- 3D
- nD (relational)
- Trees (hierarchies)
- Networks (graphs)

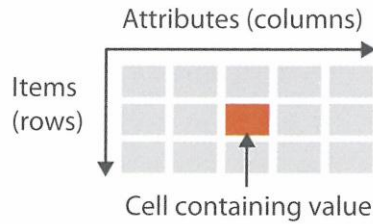


vis examples later

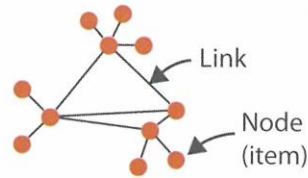


ANOTHER VIEW

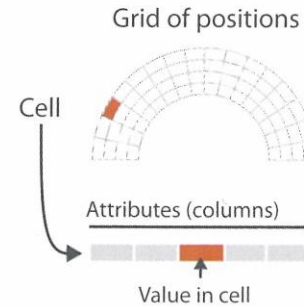
→ Tables



→ Networks



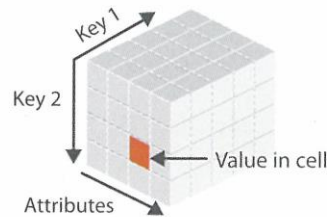
→ Fields (Continuous)



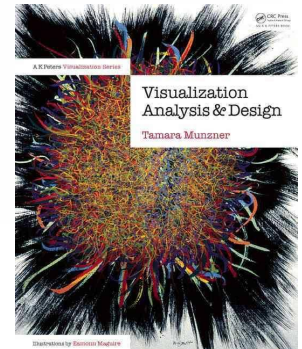
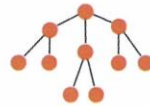
→ Geometry (Spatial)



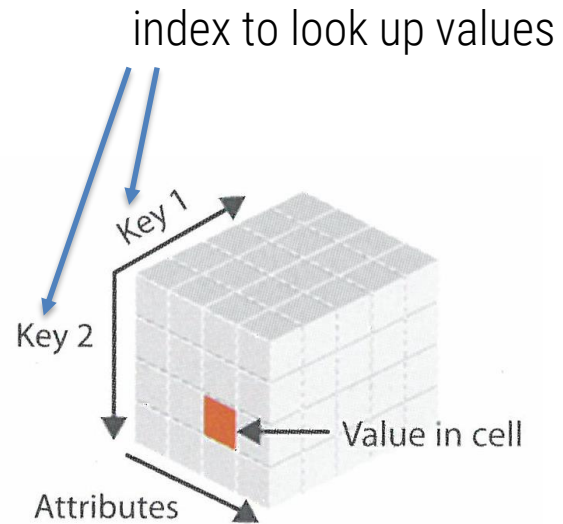
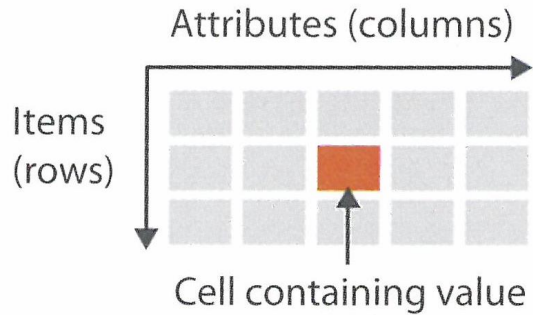
→ Multidimensional Table



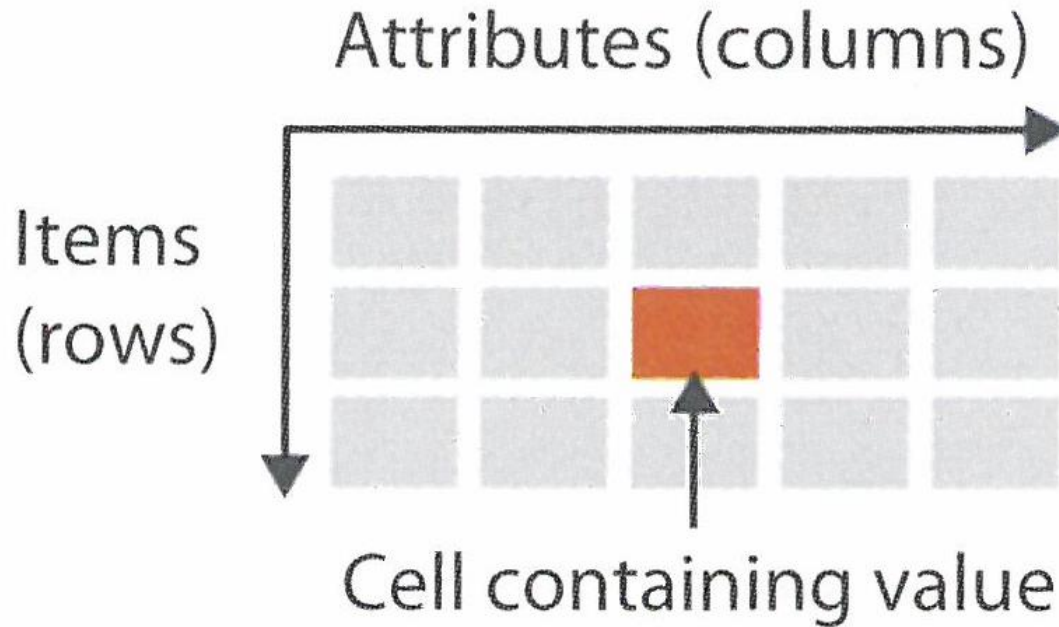
→ Trees



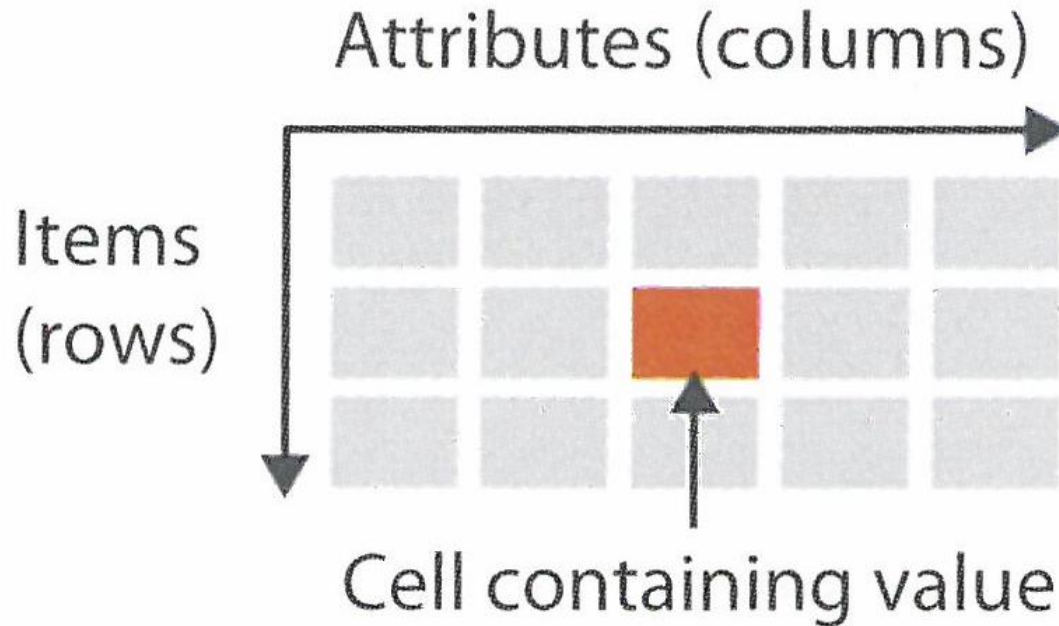
DATA TABLES - TERMINOLOGY



WHAT COULD BE THE KEY HERE?



WHAT DATA TYPE IS SUITABLE FOR A KEY?



KEYS VS. VALUES

key attributes are also sometimes called:

- independent attribute
- dimension

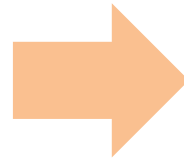
value attributes are also sometimes called:

- dependent attribute
- measure

LEVELS

= unique values for a categorical or ordered attribute

| Conference | Year | Paper.Title |
|------------|------|---------------------------|
| InfoVis | 2015 | A comparative study ... |
| InfoVis | 2015 | A Linguistic Approach... |
| InfoVis | 2015 | A Psychophysical Inv... |
| InfoVis | 2015 | A Simple Approach fo... |
| InfoVis | 2015 | Acquired Codes of Me... |
| InfoVis | 2015 | AggreSet: Rich and Sc... |
| InfoVis | 2015 | AmbiguityVis: Visuali... |
| InfoVis | 2015 | Automatic Selection ... |
| InfoVis | 2015 | Beyond Memorability... |
| InfoVis | 2015 | Beyond Weber's Law:... |
| InfoVis | 2015 | Evaluation of Parallel... |
| InfoVis | 2015 | Guidelines for Effecti... |
| InfoVis | 2015 | High-Quality Ultra-Co... |
| InfoVis | 2015 | HOLA: Human-like Ort... |
| InfoVis | 2015 | How do People Make ... |



CONFERENCE:
InfoVis, Vis, SciVis, VAST

YEAR:
1990 – 2015

PAPER.TITLE:
>2500 different

VISPUBDATA

ATTRIBUTES

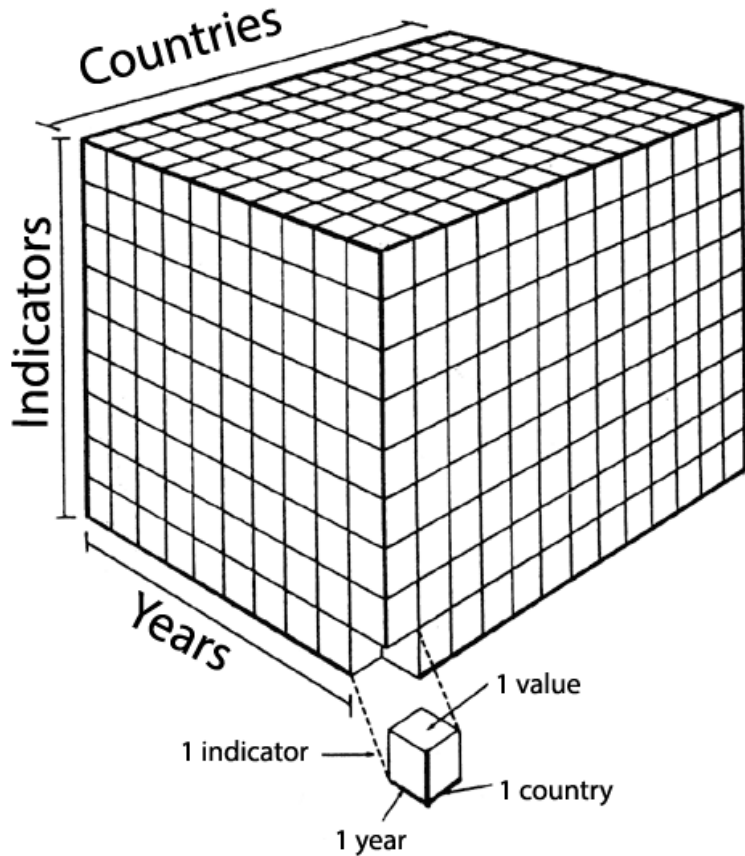


ITEMS

| # | Abc | Abc | Abc | Abc | # | # | Abc | Abc | Abc | Abc | Abc | Abc | Abc | Abc |
|------|---------------------------|----------------------|-------------------------|------------|-----------|-----------------------|---------------------------|----------------------------|----------------------------|----------------------------|----------------------|----------------------------|--------------------------|-----|
| Year | Paper.Title | Paper.DOI | Link | First.page | Last.page | Paper.type..C.conf... | Abstract | Author.Names | First.Author.Affilia... | Deduped.author.n... | References | Author.Keywords | OCR.Authors | |
| 2015 | A comparative study ... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 619 | 628 | J | RadViz and star coord... | Rubio-Sanchez, M.;Ra... | ;; | Rubio-Sanchez, M.,Ra... | 10.1109/VAST.2010... | RadViz, Star coordina... | Rubio-S ' Anchez, Ma... | |
| 2015 | A Linguistic Approach... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 698 | 707 | J | When data categorie... | Setlur, V.,Stone, M.C. | ; | Setlur, V.,Stone, M.C. | null | linguistics, natural la... | Setlur,Vidya;Stone,M... | |
| 2015 | A Psychophysical Inv... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 479 | 488 | J | Physical visualization... | Jansen, Y.;Hornbaek, K. | Univ. of Copenhagen, ... | Jansen, Y.;Hornbaek, K. | 10.1109/TVCG.2012... | Data physicalization, ... | Jansen,Yvonne;Hornb... | |
| 2015 | A Simple Approach fo... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 678 | 687 | J | General methods for ... | Simonetto, P.,Archam... | ;; | Simonetto, P.,Archam... | 10.1109/TVCG.2011... | Euler diagrams, Boun... | Simonetto,Paolo;Arc... | |
| 2015 | Acquired Codes of Me... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 509 | 518 | J | While information vis... | Byrne, L.;Angus, D.;W... | ;; | Byrne, L.;Angus, D.;W... | 10.1109/TVCG.2013... | Visual Design, Taxono... | Byrne,Lydia;Angus,D... | |
| 2015 | AggreSet: Rich and Sc... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 688 | 697 | J | Datasets commonly i... | Yalcin, M.A.;Elmqvist... | Univ. of Maryland, Co... | Yalcin, M.A.;Elmqvist... | 10.1109/TVCG.2011... | Multi-valued attribut... | Adil Yalcin, M;Beders... | |
| 2015 | AmbiguityVis: Visuali... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 359 | 368 | J | Node-link diagrams p... | Yong Wang,Qiaomu S... | ;;;;; | Yong Wang,Qiaomu S... | 10.1109/TVCG.2006... | Visual Ambiguity, Vis... | Wang,Yong;Shen,Qia... | |
| 2015 | Automatic Selection ... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 669 | 677 | J | Effective small multi... | Anand, A.,Talbot, J. | ; | Anand, A.;Talbot, J. | 10.1109/VAST.2010... | Small multiple displa... | Anand,Anushka,Talbo... | |
| 2015 | Beyond Memorability... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 519 | 528 | J | In this paper we mov... | Borkin, M.A.;Bylinskii... | ;;;;; | Borkin, M.;Bylinskii, Z... | 10.1109/TVCG.2012... | Information visualiza... | null | |
| 2015 | Beyond Weber's Law... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 469 | 478 | J | Models of human per... | Kay, M.;Heer, J. | ; | Kay, M.;Heer, J. | 10.1109/TVCG.2014... | Weber's law, percept... | Kay,Matthew;Heer,Je... | |
| 2015 | Evaluation of Parallel... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 579 | 588 | J | The parallel coordina... | Johansson, J.;Forsell... | Norrkoping Visualiza... | Johansson, J.;Forsell... | 10.1109/TVCG.2014... | Survey, evaluation, g... | Johansson,Jimmy;For... | |
| 2015 | Guidelines for Effecti... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 489 | 498 | J | Semi-automatic text ... | Strobelt, H.;Oelke, D.;... | ;;; | Strobelt, H.,Oelke, D.;... | 10.1109/TVCG.2012... | Text highlighting tec... | Strobelt,Hendrik;Oel... | |
| 2015 | High-Quality Ultra-Co... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 339 | 348 | J | Prior research into ne... | Yoghourdijan, V.;Dwy... | ;;;;; | Yoghourdijan, V.;Dwy... | 10.1109/TVCG.2008... | Network visualizatio... | Yoghourdijan,Vahan; | |
| 2015 | HOLA: Human-like Ort... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 349 | 358 | J | Over the last 50 year... | Kieffer, S.;Dwyer, T.;... | ;;; | Kieffer, S.;Dwyer, T.;... | 10.1109/TVCG.2006... | Graph layout, orthog... | Kieffer,Steve;Dwyer... | |
| 2015 | How do People Make ... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 499 | 508 | J | In this paper, we wou... | Sukwon Lee,Sung-He... | Sch. of Ind. Eng., Purd... | Sukwon Lee,Sung-He... | 10.1109/TVCG.2013... | Sensemaking model, l... | Lee,Sukwon;Kim,Sun... | |
| 2015 | Improving Bayesian R... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 529 | 538 | J | Decades of research ... | Ottley, A.;Peck, E.M.;... | ;;;;; | Ottley, A.;Peck, E.M.;... | 10.1109/TVCG.2014... | Bayesian Reasoning, ... | Ottley,Alvitta;Peck,E... | |
| 2015 | Matches, Mismatche... | 10.1109/TVCG.2015... | http://dx.doi.org/10... | 449 | 458 | J | The energy performa... | Brehmer, M.;Ng, J.,Ta... | ;;; | Brehmer, M.,Ng, J.,Ta... | 10.1109/TVCG.2011... | Design study, design... | Brehmer,Matthew;N... | |



THE DATA CUBE



| Country | Year | Child mortality | Births per woman |
|-------------|------|-----------------|------------------|
| Afghanistan | 2014 | 68.1 | 4.8 |
| Afghanistan | 2013 | 69.9 | 5.1 |
| France | 2014 | 3.6 | 2.0 |
| France | 2013 | 3.6 | 2.0 |
| USA | 2014 | 5.7 | 5.9 |
| USA | 2013 | 1.9 | 1.9 |

MULTI-ATTRIBUTE DATA – OUR VIEW TODAY

$n \times d$ matrix

n attributes

d items (data points)

| Country | Year | Child mortality | Births per woman |
|-------------|------|-----------------|------------------|
| Afghanistan | 2014 | 68.1 | 4.8 |
| Afghanistan | 2013 | 69.9 | 5.1 |
| France | 2014 | 3.6 | 2.0 |
| France | 2013 | 3.6 | 2.0 |
| USA | 2014 | 5.7 | 5.9 |
| USA | 2013 | 1.9 | 1.9 |

ARRANGING TABULAR DATA

In Space

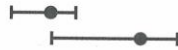
WHY ARRANGING DATA

➔ Magnitude Channels: Ordered Attributes

Position on common scale



Position on unaligned scale



Length (1D size)



Tilt/angle



Area (2D size)



Depth (3D position)



Color luminance



Color saturation



Curvature



Volume (3D size)



Same

Same

Same

Effectiveness
Most
Least

➔ Identity Channels: Categorical Attributes

Spatial region



Color hue



Motion



Shape



QUANTITATIVE VALUES

APPROACH

- Let's start with two attributes:
country & income per person

| Country | Income per person |
|-------------|-------------------|
| Afghanistan | 850 |
| France | 29500 |
| US | 41000 |

1. FIND A LAYOUT

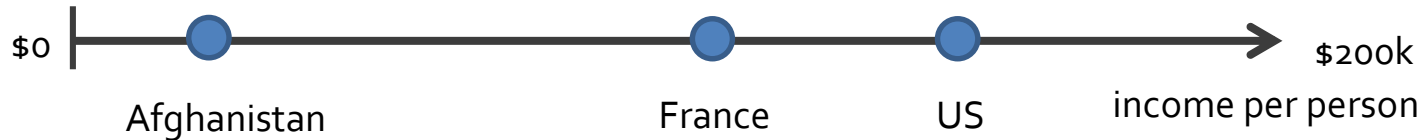


| Country | Income per person |
|-------------|-------------------|
| Afghanistan | 850 |
| France | 29500 |
| US | 41000 |



2. CHOOSE A VISUAL ENCODING & MARK

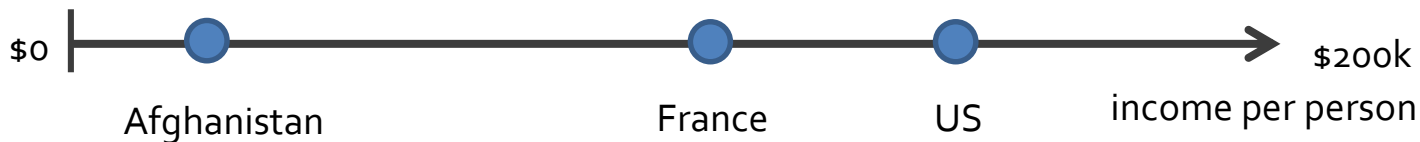
E.g. position + circle



1. FIND A LAYOUT

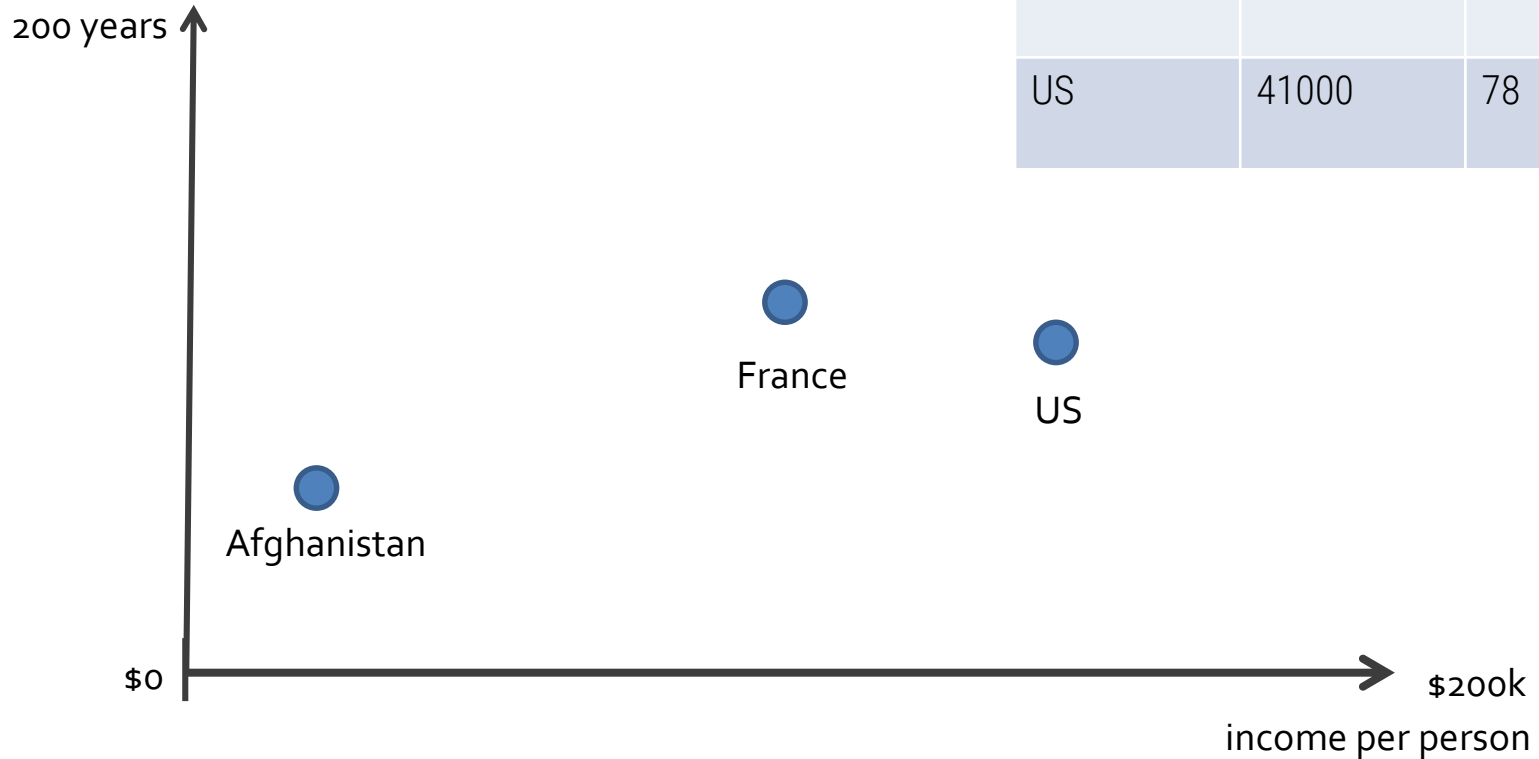
| Country | Income per person | Life expectancy |
|-------------|-------------------|-----------------|
| Afghanistan | 850 | 57 |
| France | 29500 | 81 |
| US | 41000 | 78 |

How do we extend this to 3 data attributes?



1. FIND A LAYOUT

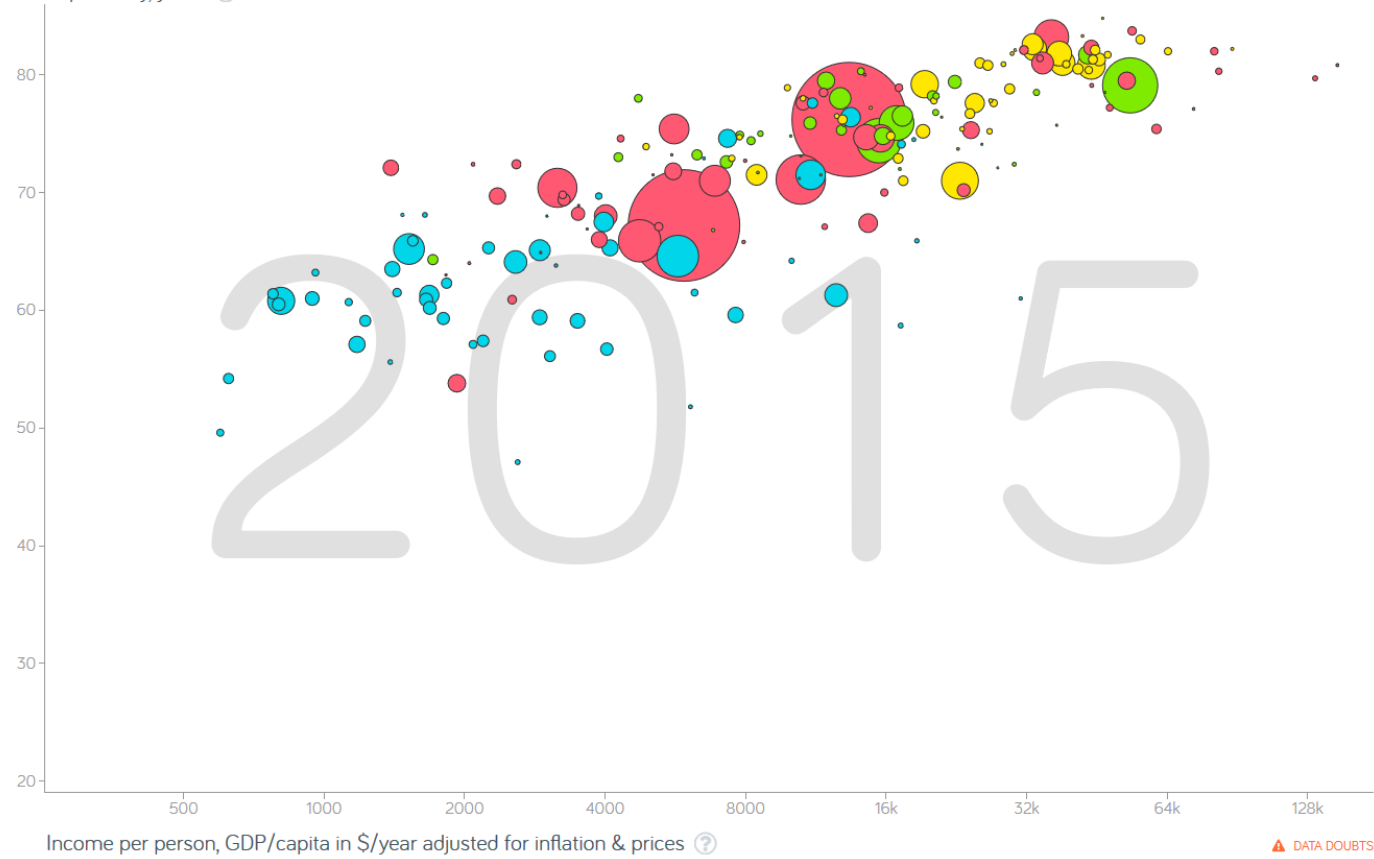
| Country | Income per person | Life expectancy |
|-------------|-------------------|-----------------|
| Afghanistan | 850 | 57 |
| France | 29500 | 81 |
| US | 41000 | 78 |



SCATTERPLOTS

- two quantitative values
- horizontal and vertical spatial dimensions
- mark type = point

Life expectancy, years ?



Color World Regions ?

Select Search...

- Afghanistan
- Albania
- Algeria
- Andorra
- Angola
- Antigua and Barbuda
- Argentina
- Armenia
- Aruba
- Australia
- Austria
- Azerbaijan
- Bahamas
- Bahrain
- Bangladesh
- Barbados
- Belarus
- Belgium
- Belize
- Benin

Size Population ?

Zoom 🔍 🔍 🔍 100%

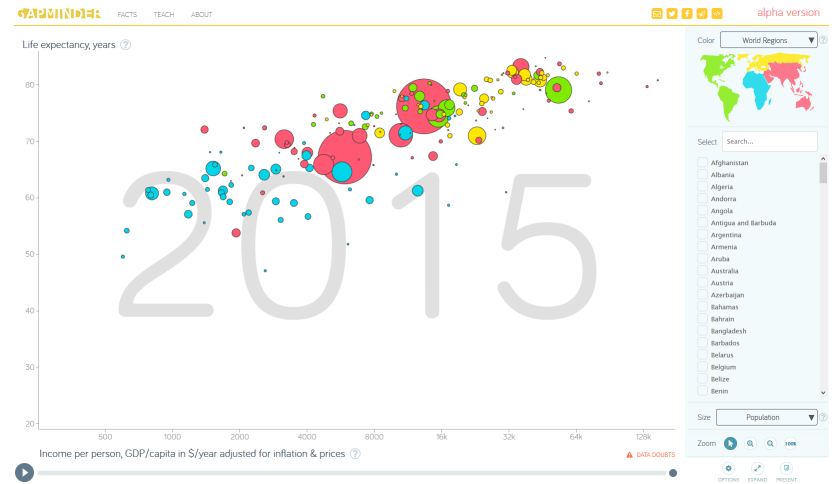
⚙️ 📏 🖨️
 OPTIONS EXPAND PRESENT



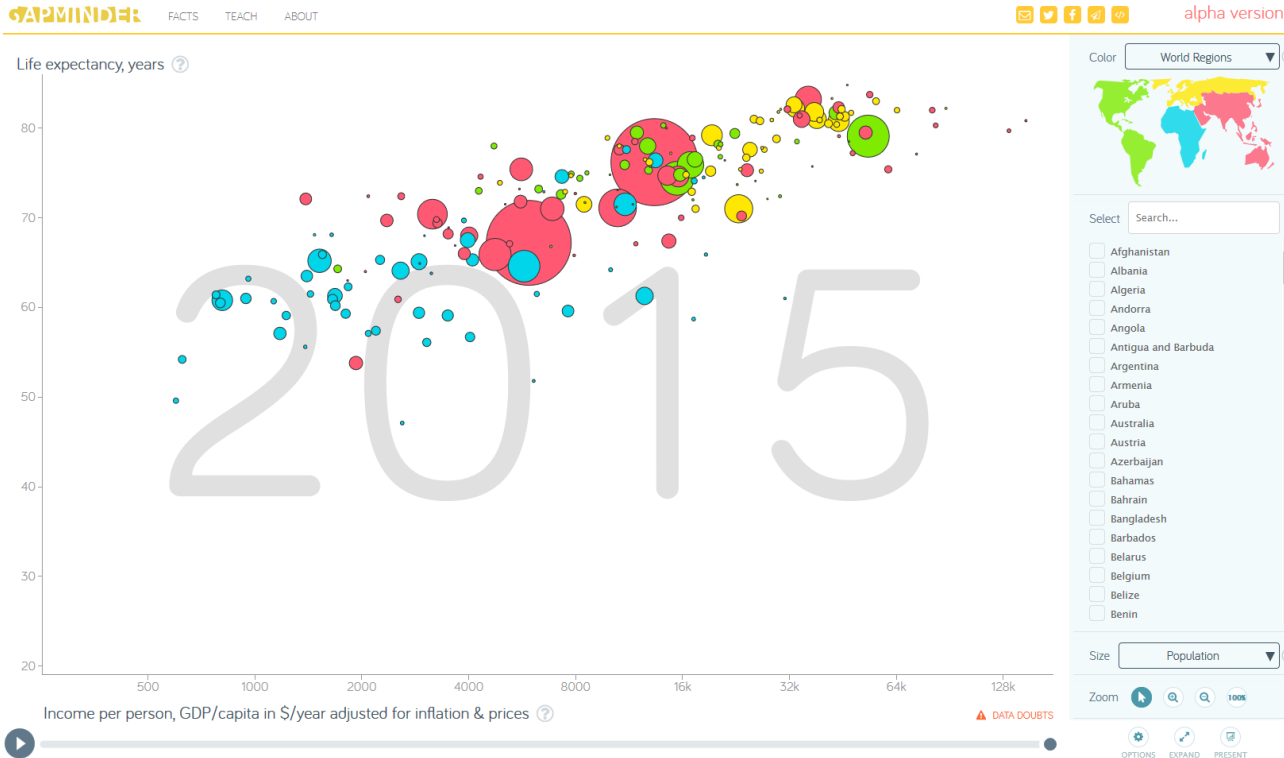
when marks are sized, the chart is often called a bubble chart or bubble plot

TASKS

- find trends
- find outliers
- show distribution
- show correlation
- locate clusters



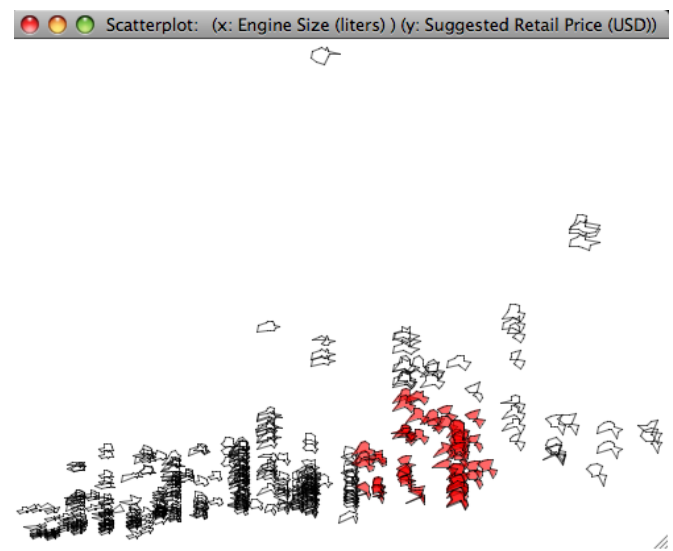
how many items are reasonable to put on a scatterplot?



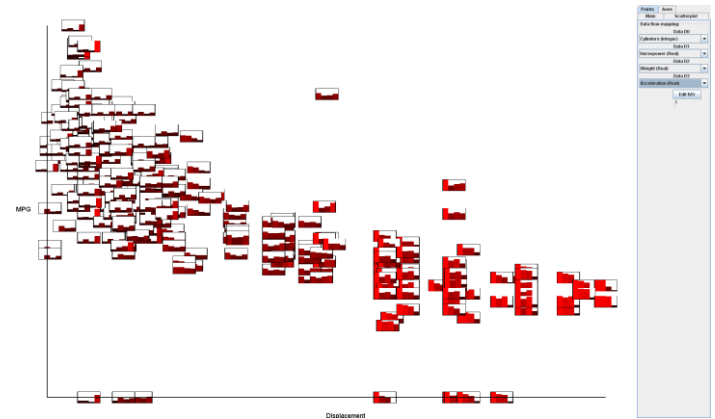
GLYPHS

marks can be replaced with glyphs

glyphs are themselves composed of multiple marks



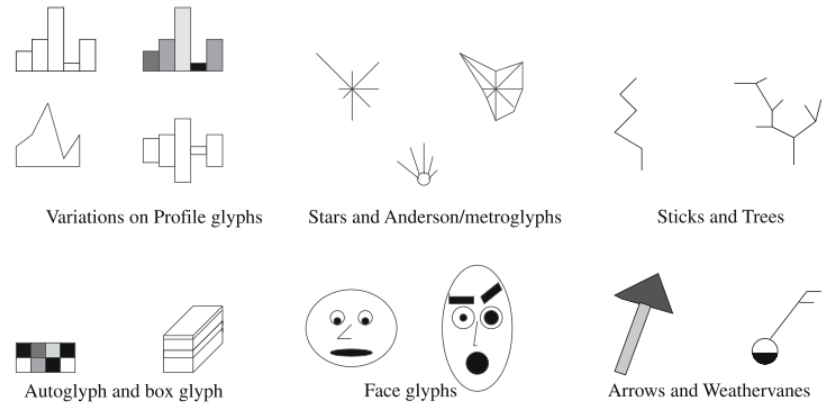
<http://rosuda.org/software/Gauguin/gauguin.html>



<https://engineering.purdue.edu/~elm/projects/gpuvis.html>

GLYPHS

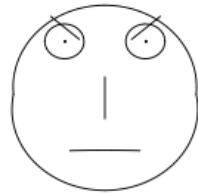
- Small composite visual representations of multi-dimensional data points
- Characterized generally by lack of reference structures (grid lines, axes labels, ...)



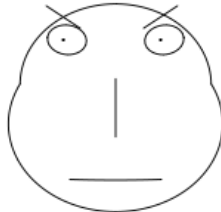
From Ward, 2002

A taxonomy of glyph placement strategies for multidimensional data visualization

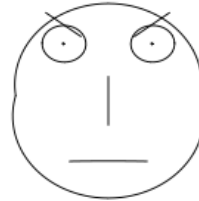
EXAMPLE: CHERNOFF FACES



AARONSON, L.H.



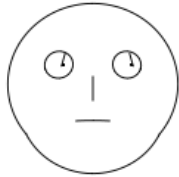
ALEXANDER, J.M.



ARMENTANO, A.J.



BERDON, R.I.



BRACKEN, J.J.



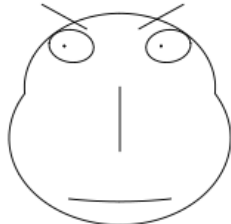
BURNS, E.B.



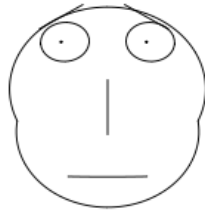
CALLAHAN, R.J.



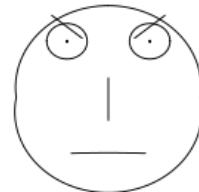
COHEN, S.S.



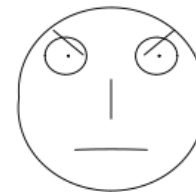
DALY, J.J.



DANNEHY, J.F.



DEAN, H.H.



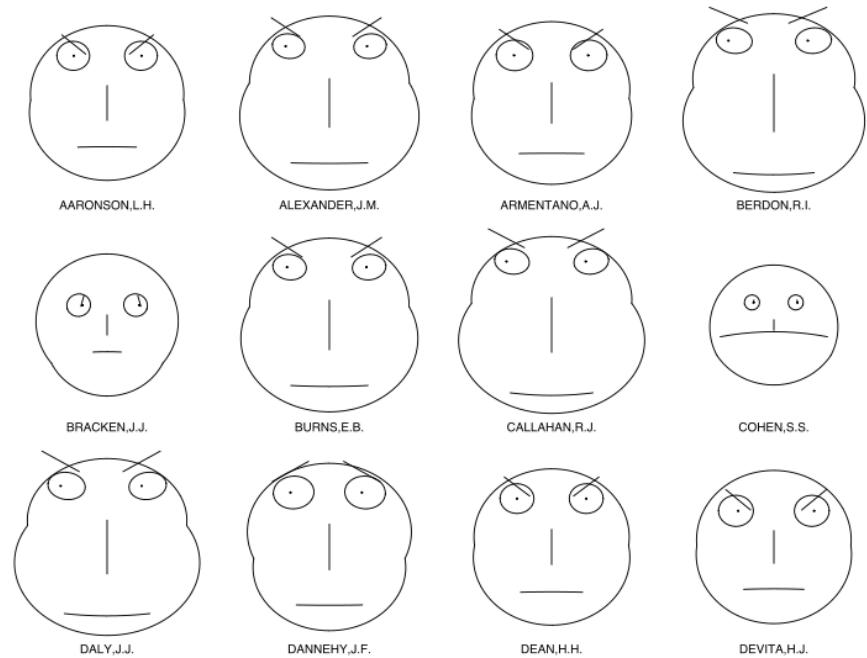
DEVITA, H.J.

Image source: Wikipedia

Herman Chernoff, [The Use of Faces to Represent Points in K-Dimensional Space Graphically](#), 1973.

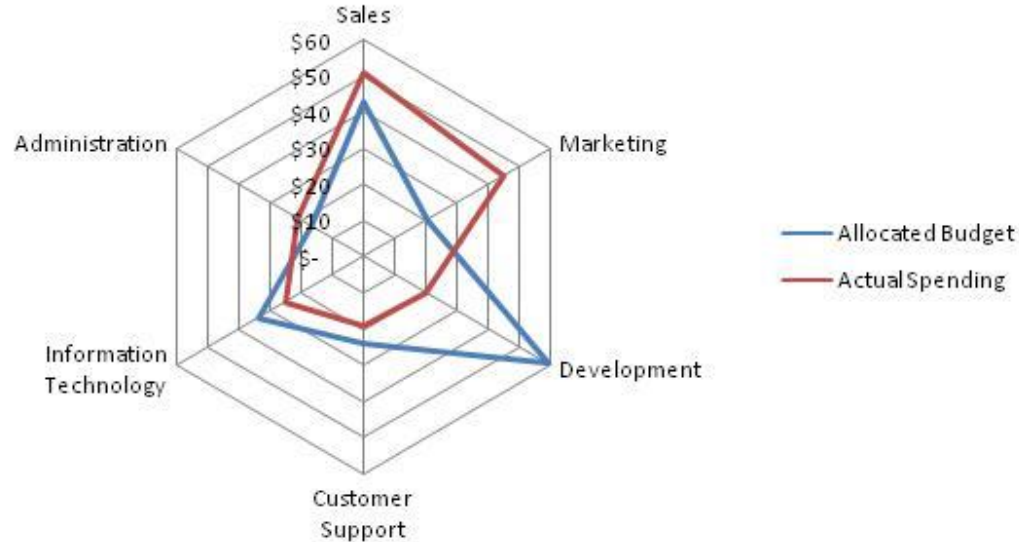
CHERNOFF FACES

- features of a human face encode data values (e.g. slant of eye brows, size of eyes, ...)
- reasoning: humans are good at differentiating faces and reading face features
- problem: chernoff faces have generally been found not to be very effective

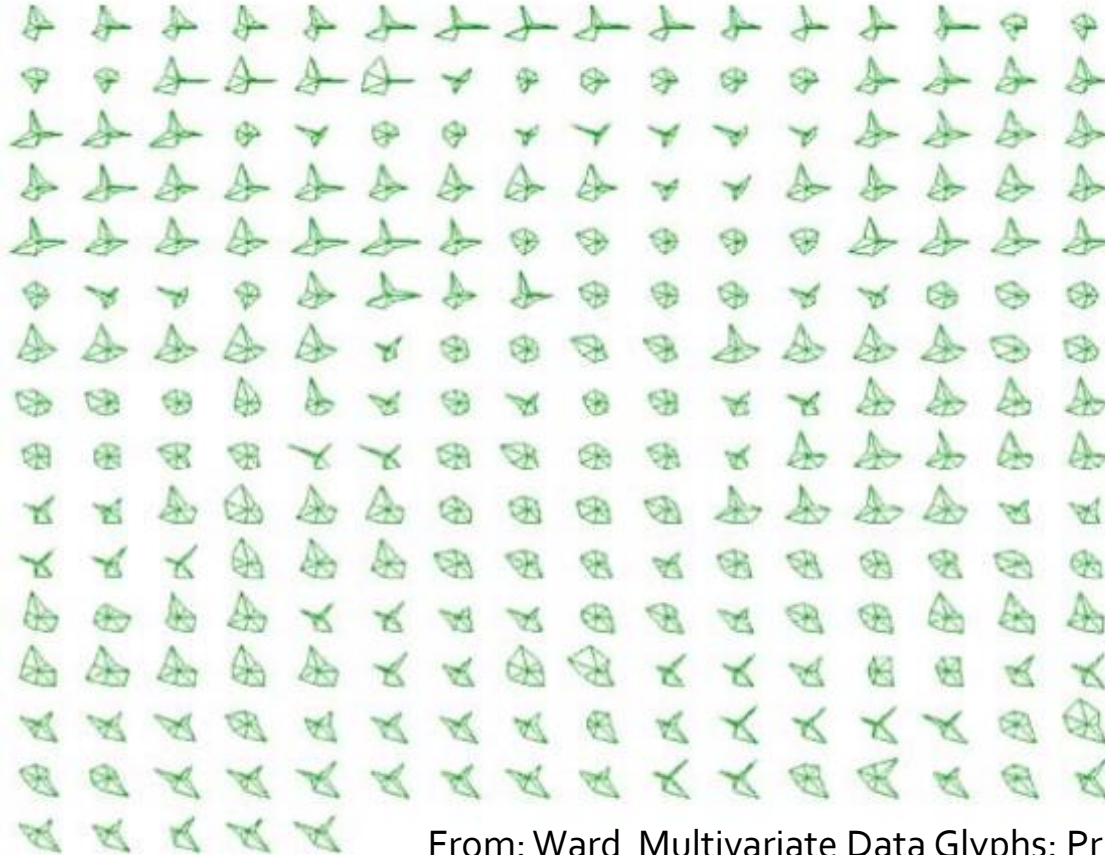


EXAMPLE: STAR GLYPHS

- Lay out dimension in radial fashion
- Draw each point as a ring



STAR GLYPHS



From: Ward Multivariate Data Glyphs: Principles and Practice. Handbook of Data Visualization (2008)

SHOW CATEGORICAL REGIONS

Separate, Order, and Align

CATEGORICAL VALUES

- spatial position is an ordered magnitude visual channel
- categorical attributes are unordered identities (no magnitude)
- cannot be encoded with spatial position
- BUT: can be expressed with a spatial region

REGIONS

- contiguous bounded areas
- distinct from one another
- need to be separated, ordered, and aligned



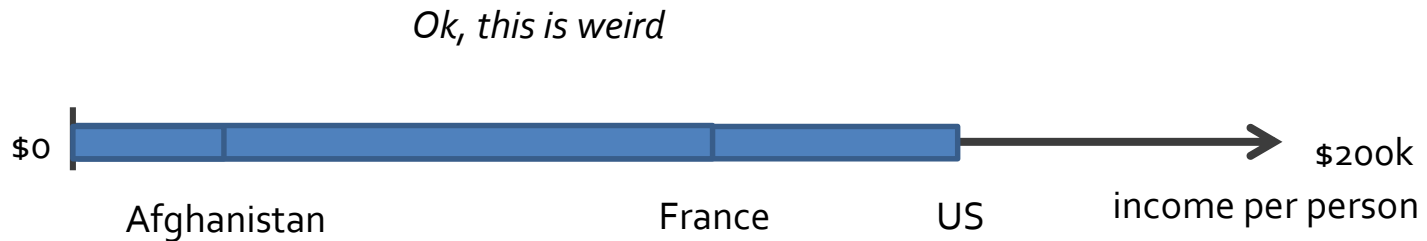
LIST ALIGNMENT

ONE KEY

LIST ALIGNMENT

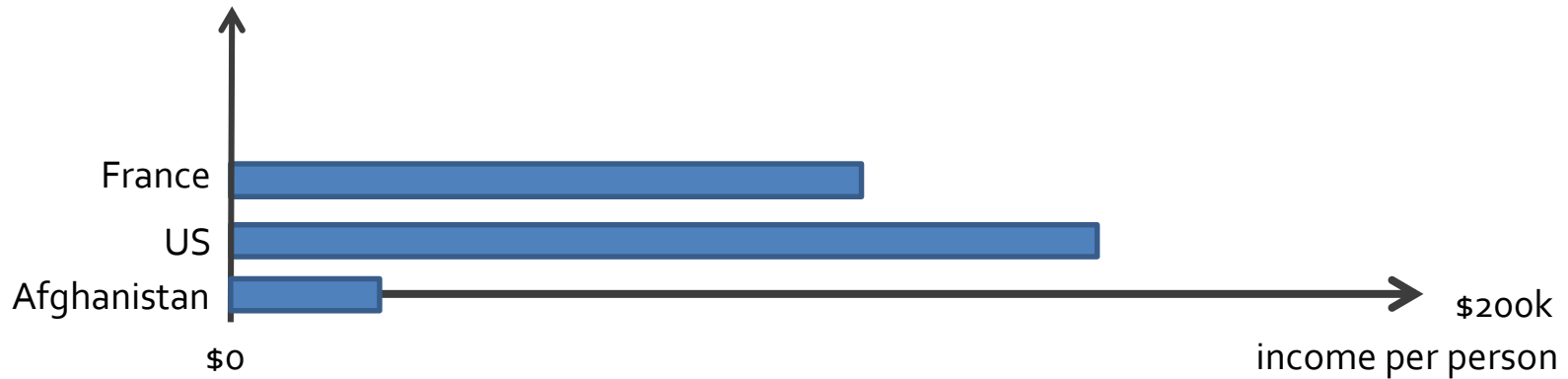
separate into regions by key

E.g. length + rectangle



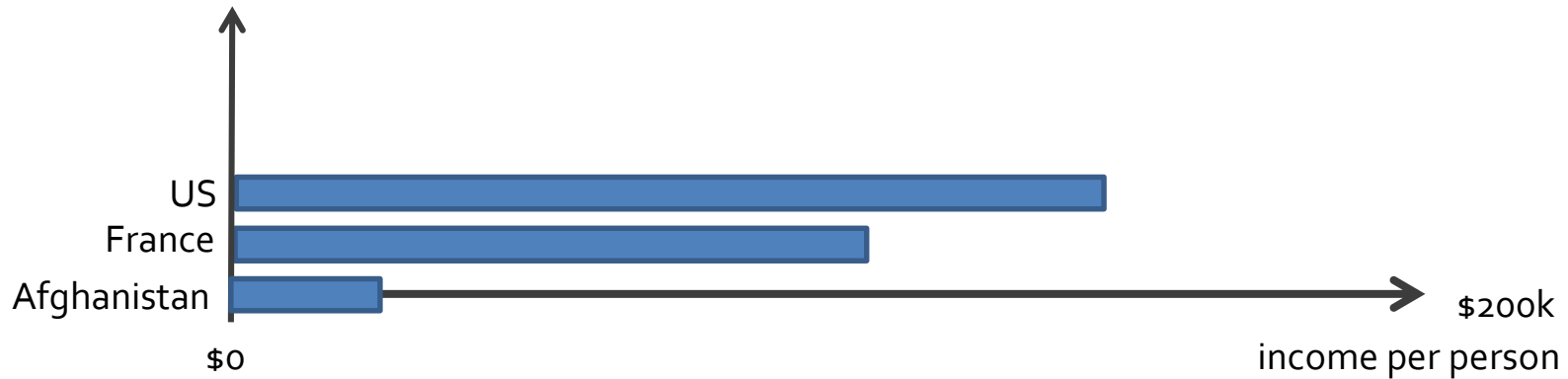
ALIGN

align regions of key categorical values along one axis in a common frame



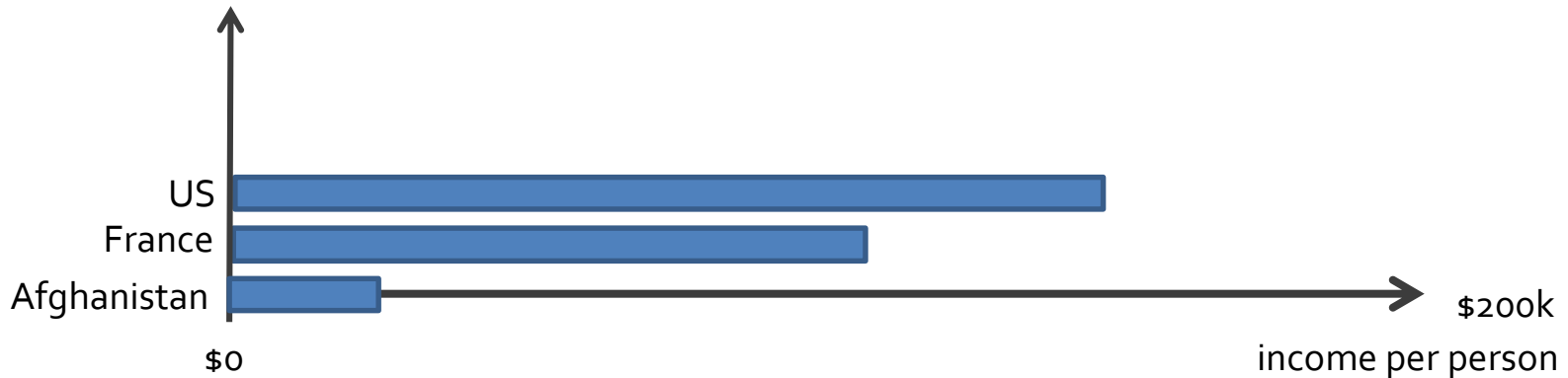
ORDER

- using a derived attribute such as alphabet
- and/or using dependent data values

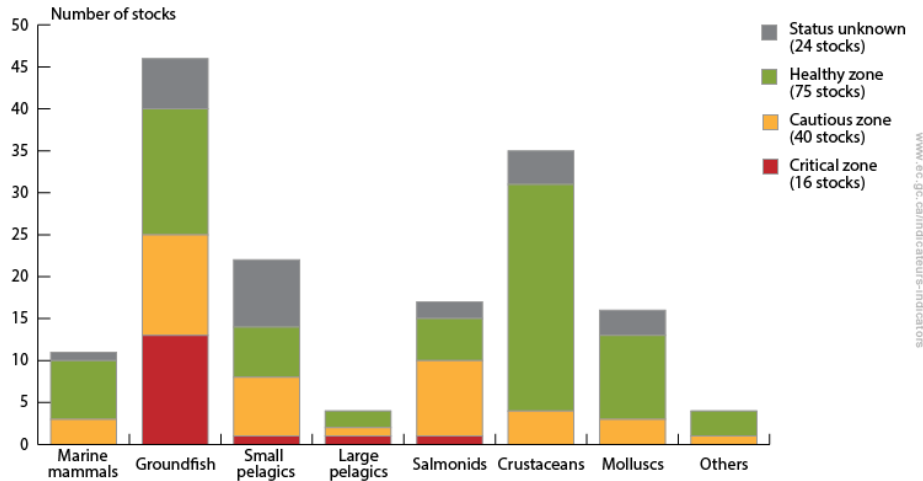


BAR CHARTS

| | |
|--------|--|
| DATA | one quantitative value attribute, one categorical key attribute |
| ENCODE | line marks, express value attribute with aligned vertical position (length), separate key attribute with horizontal position |
| TASK | lookup and compare values |
| SCALE | key attribute: dozens to hundreds of levels |



ALTERNATIVE

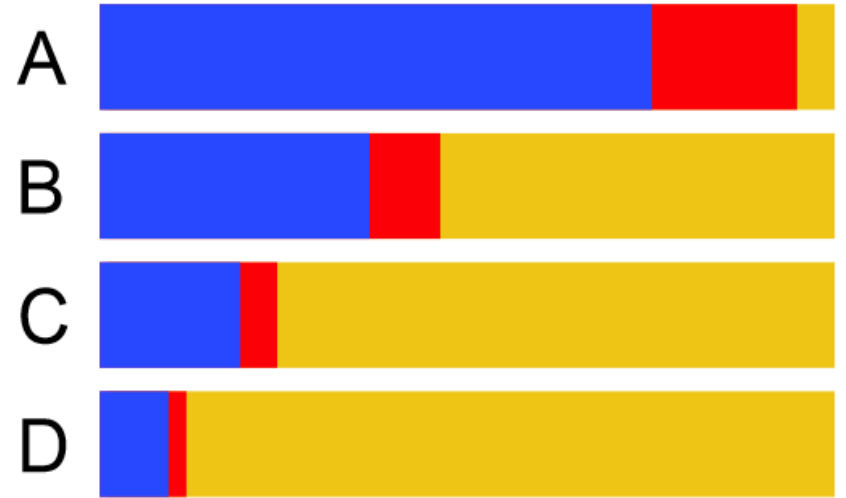
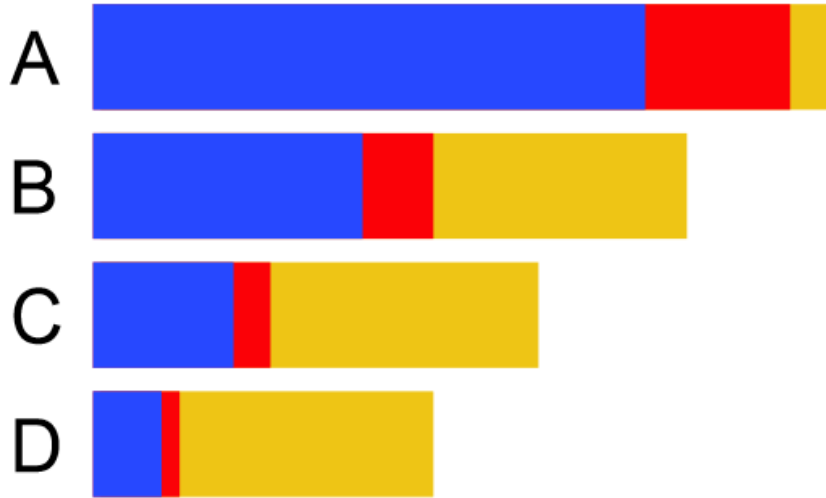


<https://www.ec.gc.ca/indicateurs-indicators/default.asp?lang=en&n=1BCD421B-1>

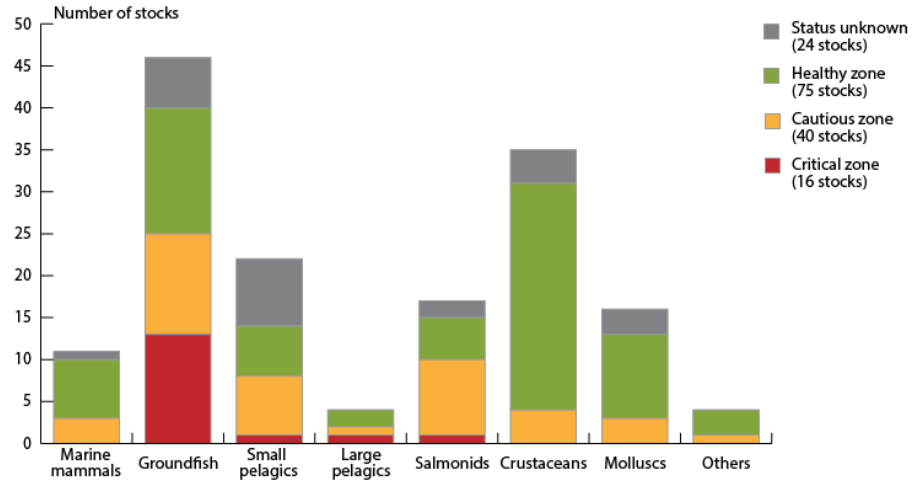
Stacked bar chart

- each bar is a composite glyph
- each bar part encodes a value
- composite glyphs arranged as a list according to primary key
- color used to distinguish secondary key
- typically used for absolute values (use a normalized stacked bar for proportions)

STACKED BARS VS. NORMALIZED STACKED BARS



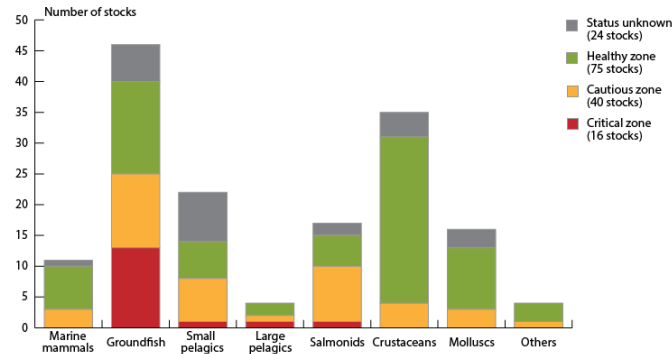
STACKED BARS



- ADVANTAGE
 - can compare totals and lowest level well
- DISADVANTAGE
 - upper levels of secondary key require comparison against non-aligned scale

STACKED BARS

| | |
|--------|---|
| DATA | MD table; one quantitative value attribute, two categorical key attributes |
| ENCODE | bar glyph: length-encoded subcomponents for each level of secondary key attribute separate bars by category of primary key |
| TASK | part-to-whole relationship, lookup values, find trends |
| SCALE | key attribute (main axis): dozens to hundreds of levels key attribute (stacked glyph axis): several to one dozen |



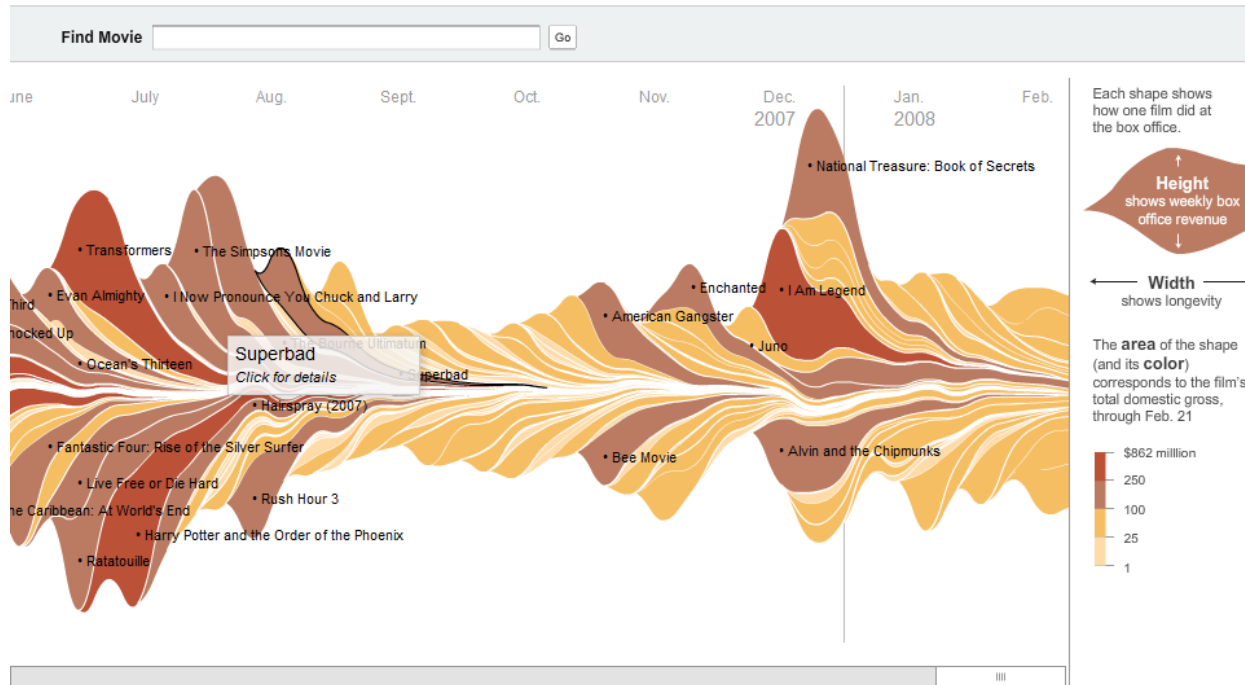
STREAMGRAPH

February 23, 2008

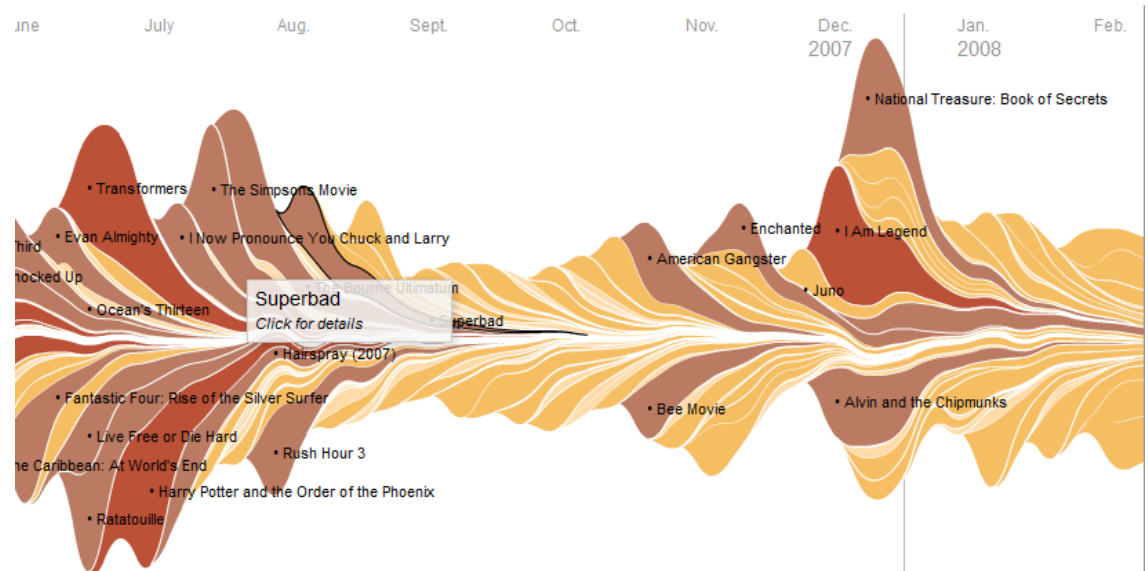
[SIGN IN TO E-MAIL OR SAVE THIS](#) | [FEEDBACK](#)

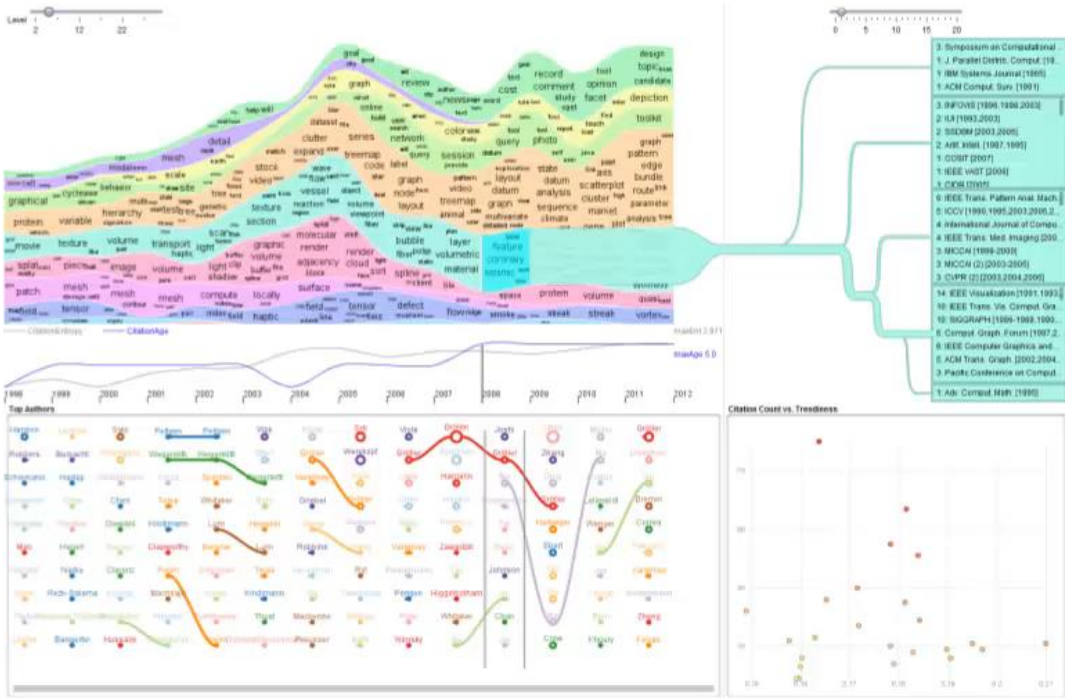
The Ebb and Flow of Movies: Box Office Receipts 1986 — 2008

Summer blockbusters and holiday hits make up the bulk of box office revenue each year, while contenders for the Oscars tend to attract smaller audiences that build over time. Here's a look at how movies have fared at the box office, after adjusting for inflation.



| | |
|--------|--|
| DATA | MD table; one quantitative value attribute (e.g. counts), one ordered key attribute (e.g. time), one categorical key attribute (e.g. film) |
| DERIVE | order of layers is derived from a quantitative attribute |
| ENCODE | use derived geometry to show layers across time, layer height encodes count |
| SCALE | key attributes (time, main axis): hundreds of time points key attributes (short axis): dozens to hundreds |





CiteRivers

Florian Heimerl, Qi Han,
Steffen Koch, Thomas Ertl

University of Stuttgart

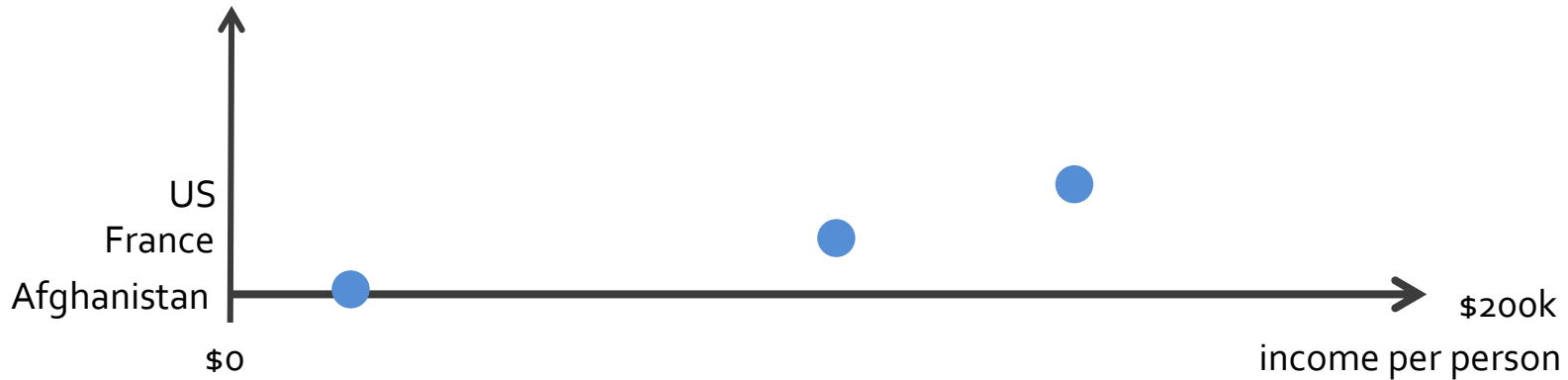
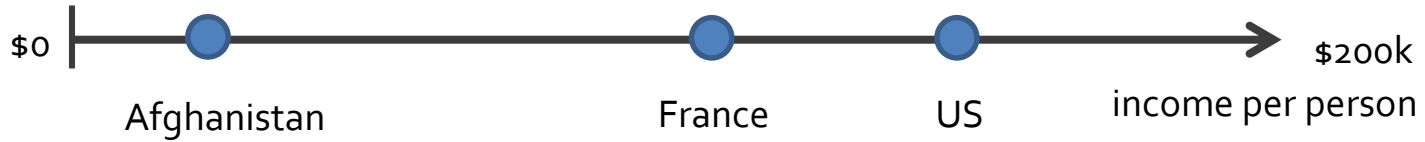
florian.heimerl@vis.uni-stuttgart.de

IEEE VAST 2015



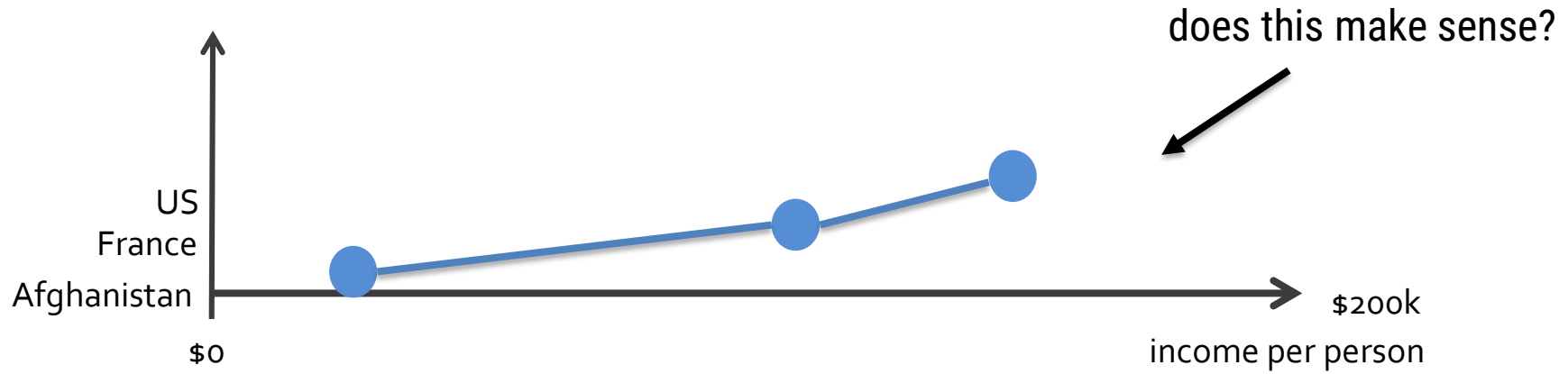
Institute for Visualization
and Interactive Systems

DOT CHART/PLOT

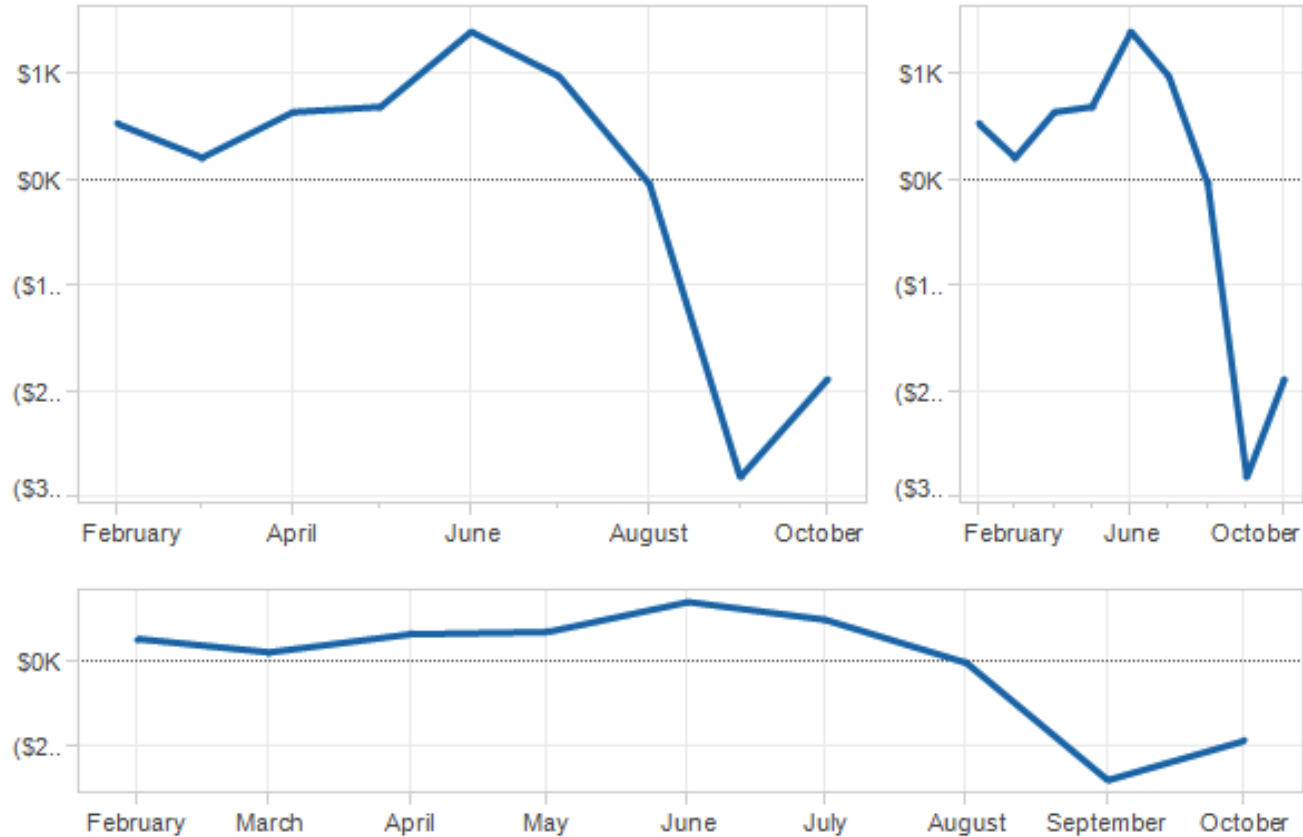


LINE CHART

augment with line connection marks
emphasize the ordering and show trends
should not be used with categorical keys



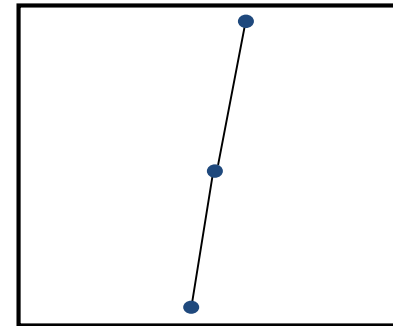
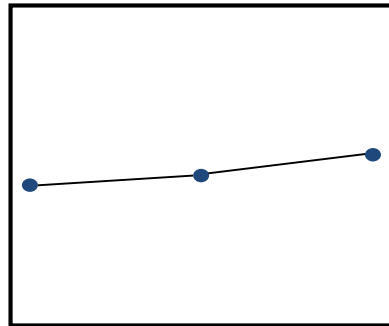
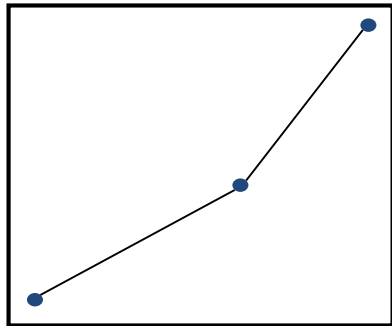
ASPECT RATIO SELECTION



BANKING TO 45°

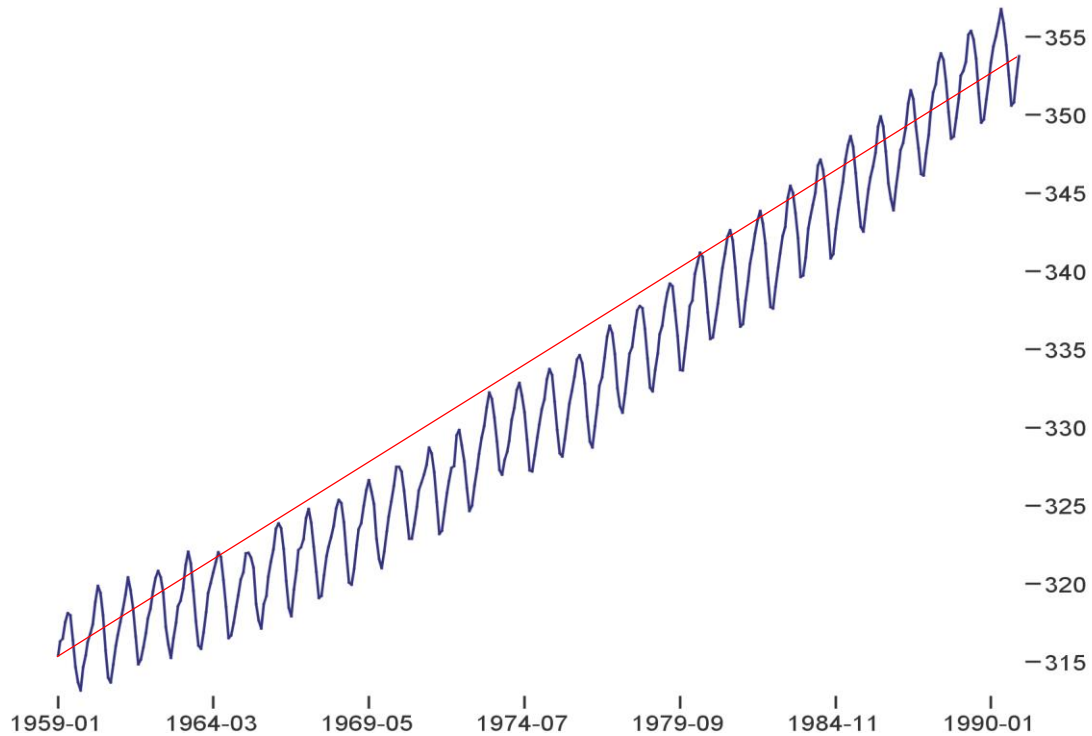
[Cleveland]

TO FACILITATE PERCEPTION OF TRENDS,
MAXIMIZE THE DISCRIMINABILITY OF LINE
SEGMENT ORIENTATIONS

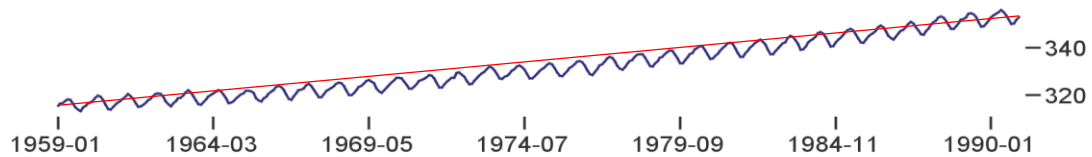


TWO SEGMENTS ARE MAXIMALLY DISCRIMINABLE WHEN THEIR AVG ABSOLUTE ANGLE IS
45°

OPTIMIZE THE *ASPECT RATIO* TO BANK TO 45°

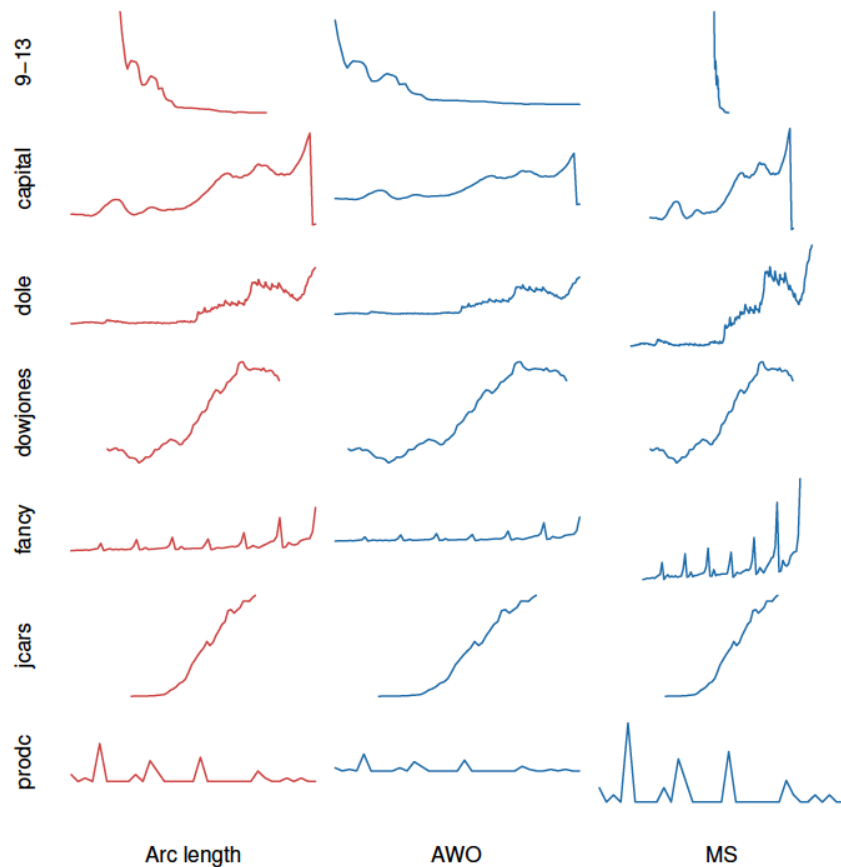


ASPECT RATIO = 1.17



ASPECT RATIO = 7.87

ALTERNATIVE METHODS



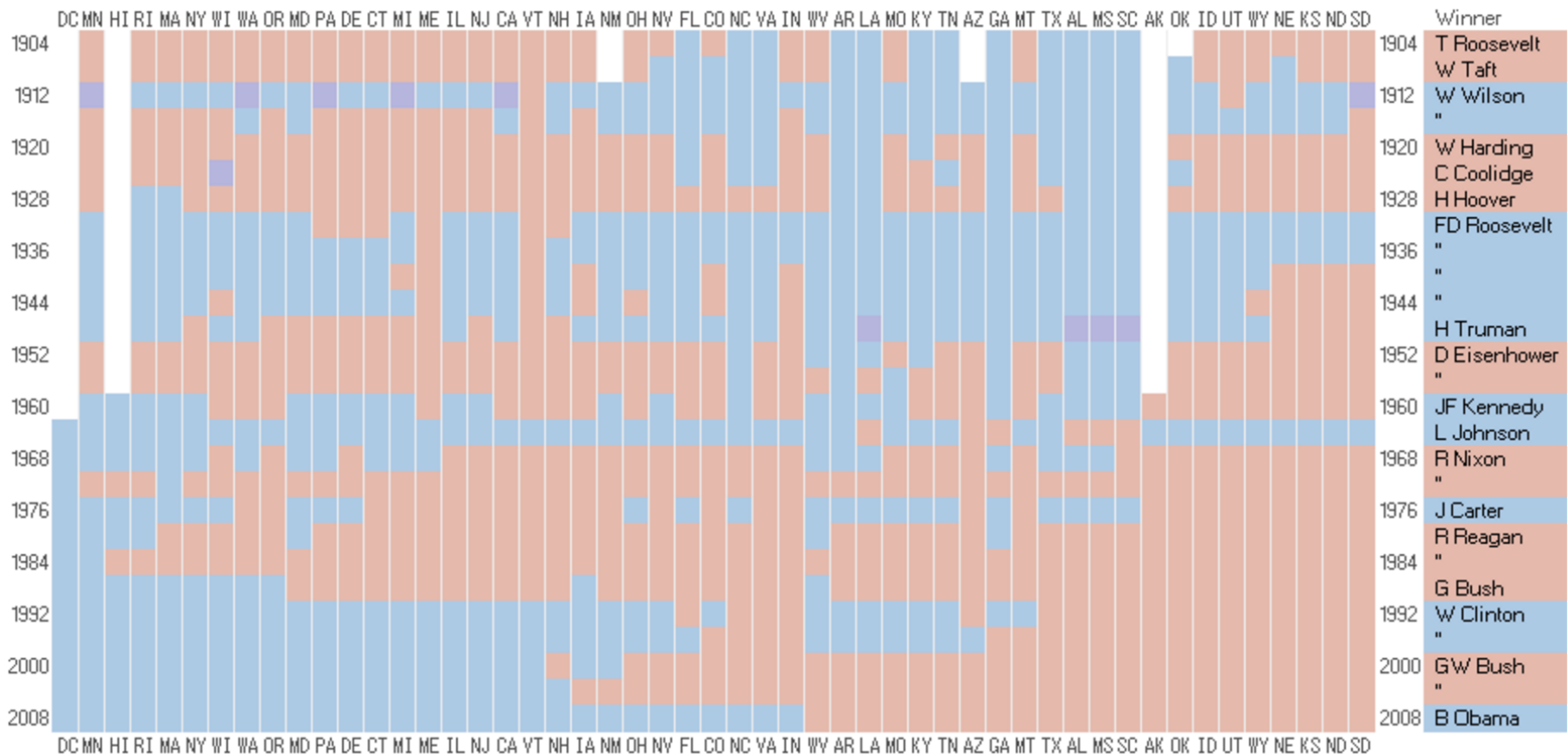
Practical advice:

CHOOSE AN **ASPECT RATIO** THAT
EMPHASIZES THE IMPORTANT DETAILS
FOR YOUR TASK

[TALBOT ET AL, 2011]

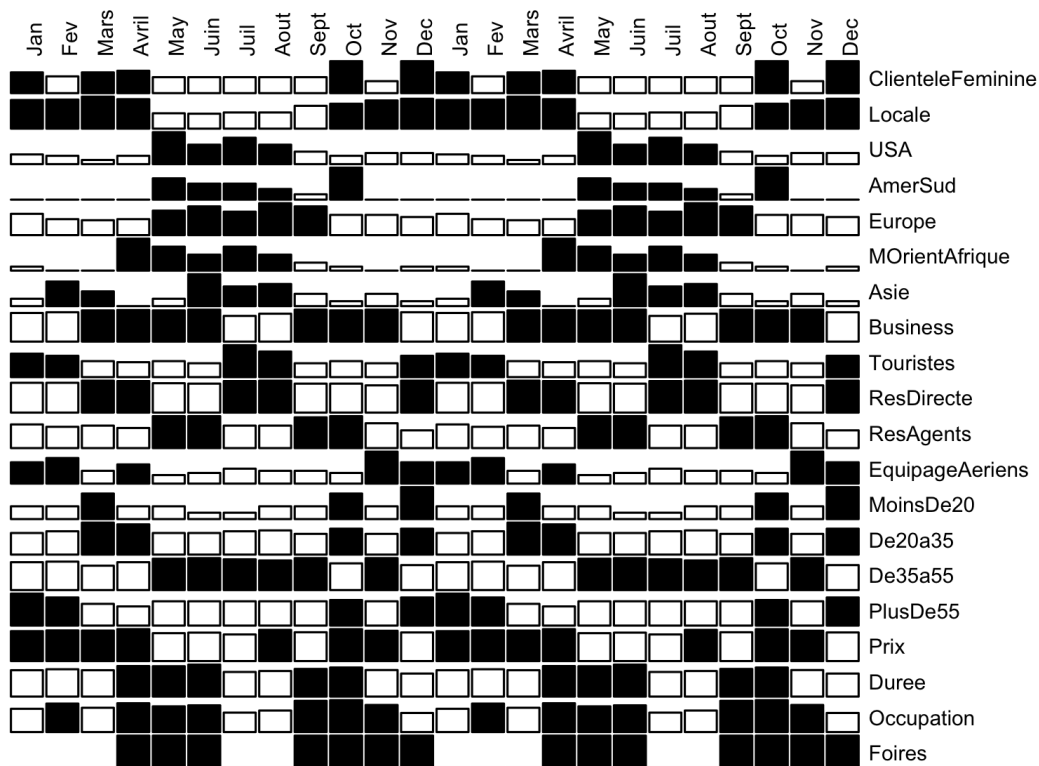
MATRIX ALIGNMENT

Two keys

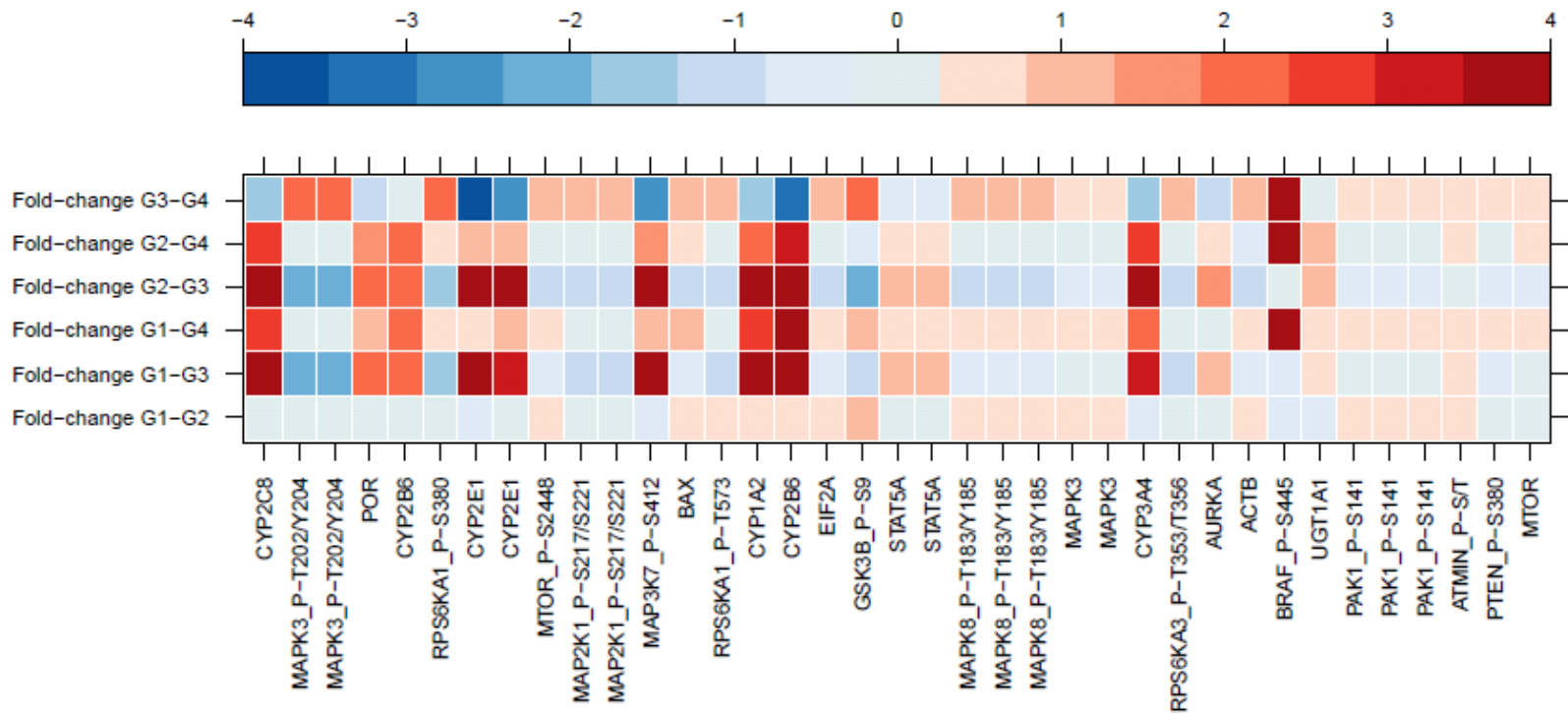


HEATMAP

Hotel 2

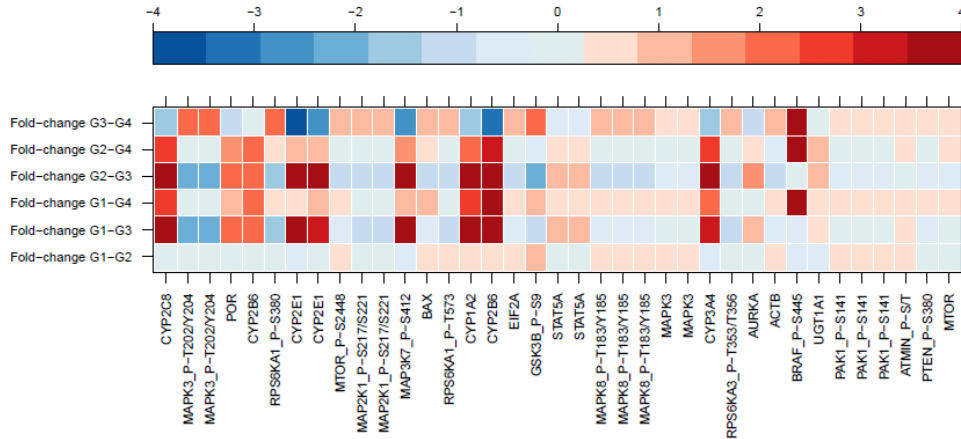


HEATMAP

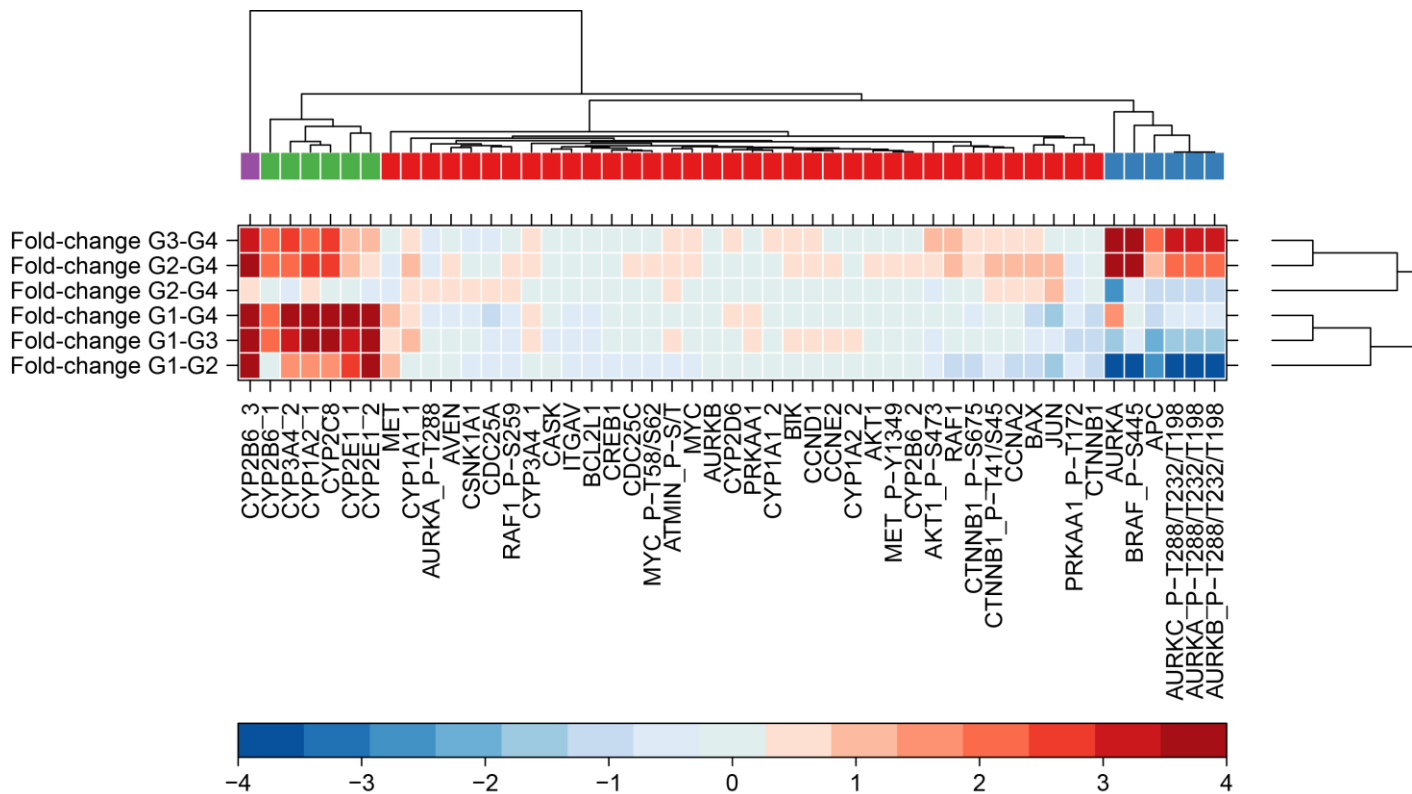


HEATMAP

| | |
|--------|---|
| DATA | Table; two categorical key attributes, one quantitative value attribute |
| ENCODE | 2D matrix alignment of area marks, e.g. with diverging color map |
| TASK | find clusters, outliers; summarize |
| SCALE | items: ~1 million (on 1000x1000px), categorical attribute levels: hundreds, quantitative attribute levels: 3-11 |



CLUSTERED HEATMAP



BACK TO OUR ORIGINAL EXAMPLE

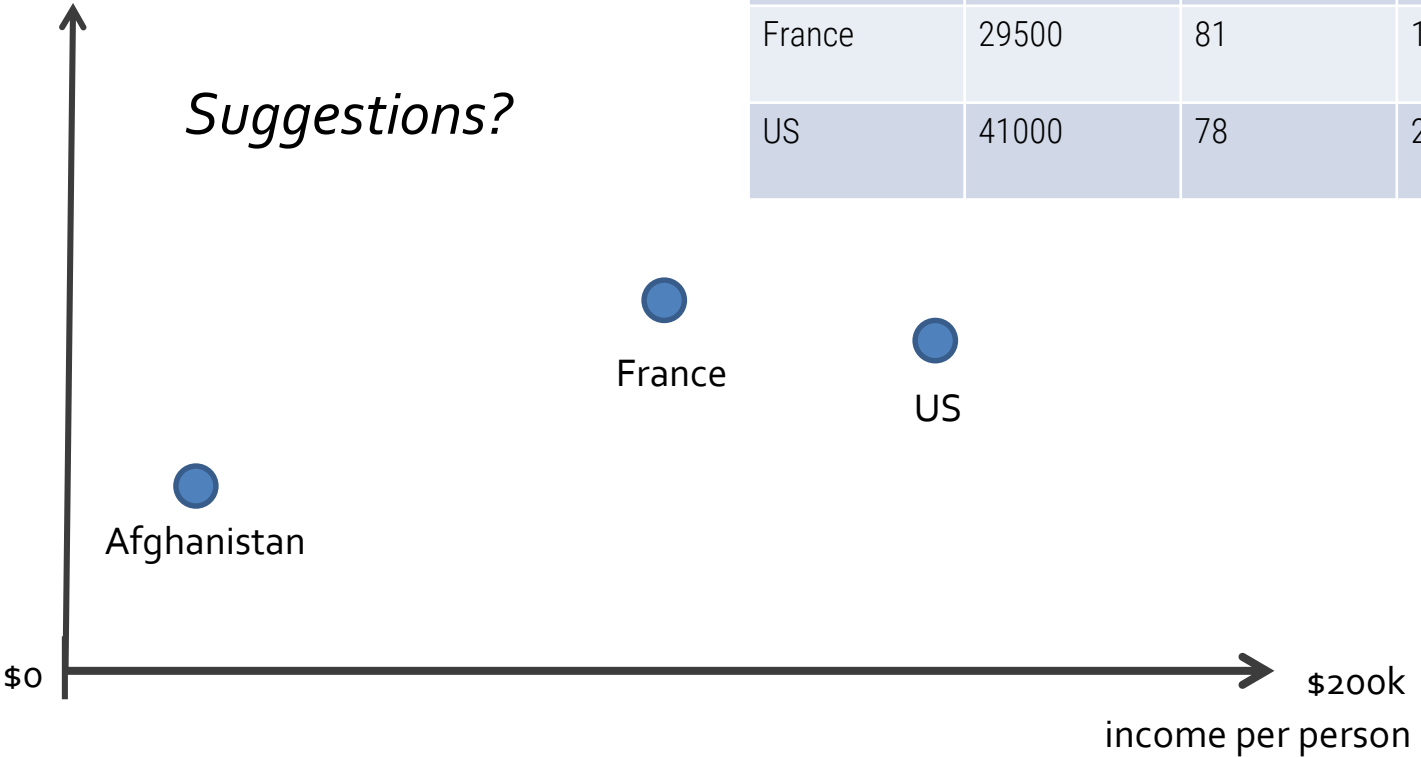
| Country | Income per person | Life expectancy | Children per woman |
|-------------|-------------------|-----------------|--------------------|
| Afghanistan | 850 | 57 | 7.1 |
| France | 29500 | 81 | 1.9 |
| US | 41000 | 78 | 2.1 |

now with 4 attributes

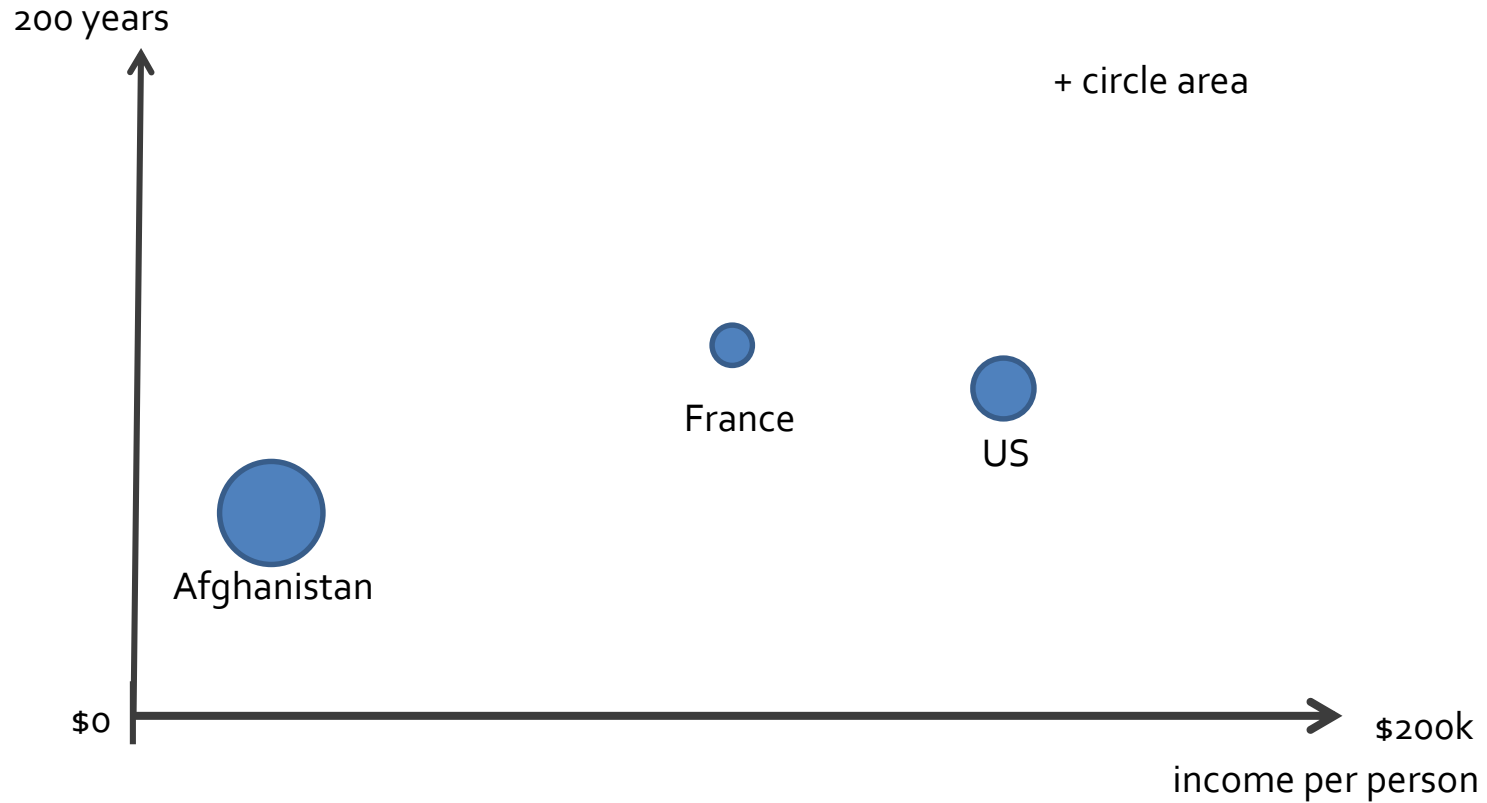
| Country | Income per person | Life expectancy | Children per woman |
|-------------|-------------------|-----------------|--------------------|
| Afghanistan | 850 | 57 | 7.1 |
| France | 29500 | 81 | 1.9 |
| US | 41000 | 78 | 2.1 |

200 years

Suggestions?

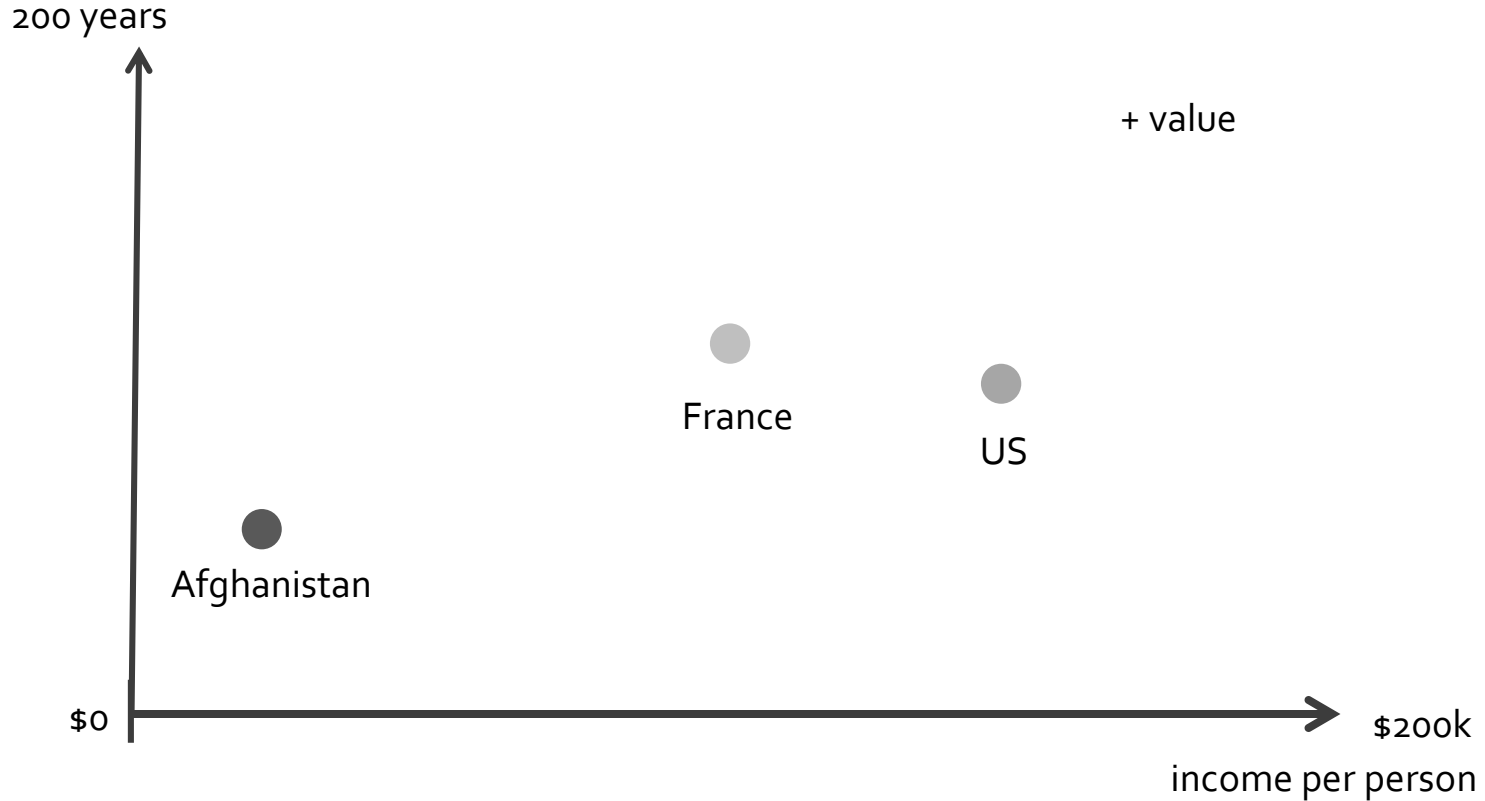


ADD ANOTHER VISUAL ENCODING



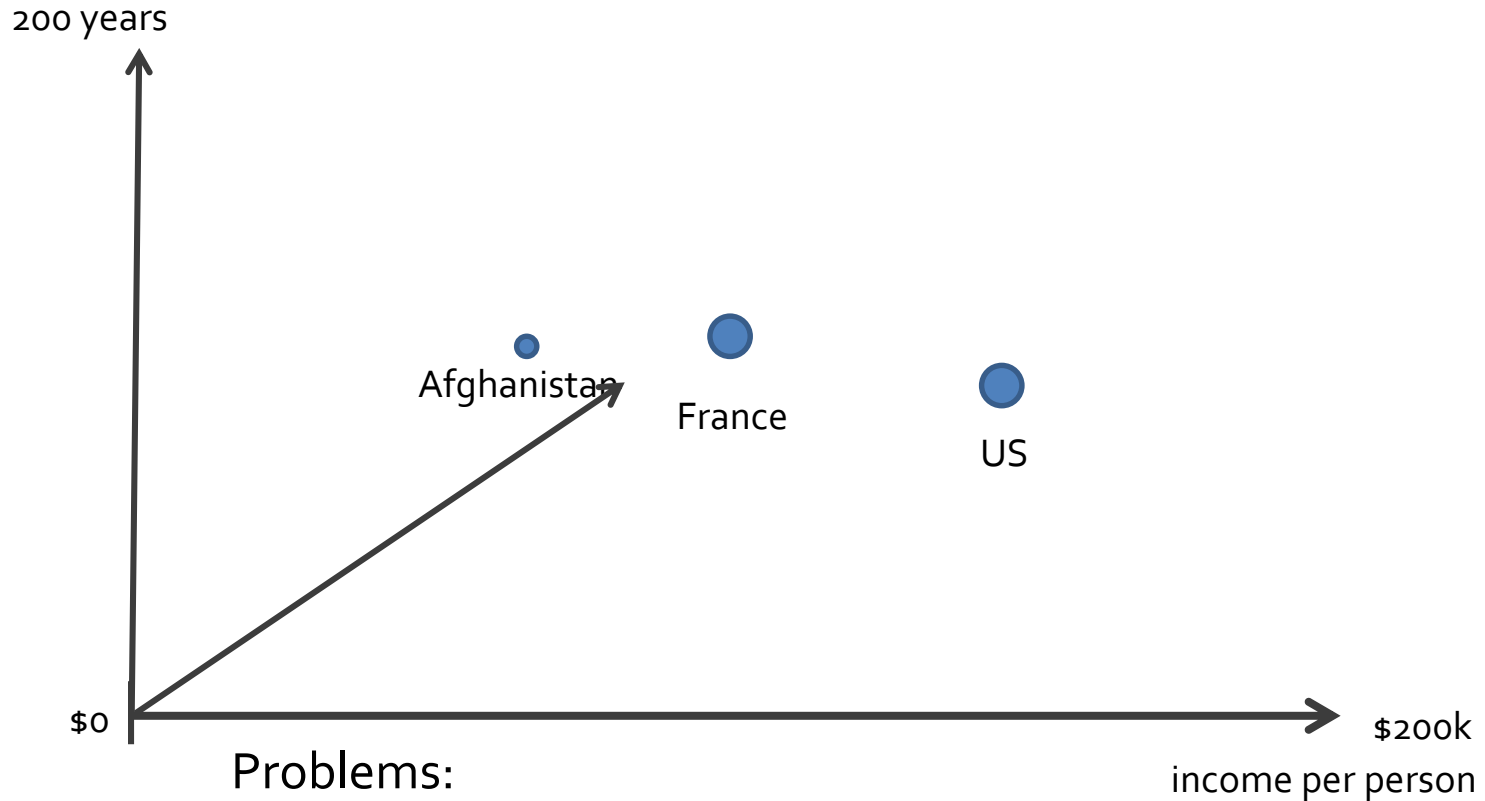
Problem:
Does not scale well to more attributes

ADD ANOTHER VISUAL ENCODING



Problem:
Does not scale well to more attributes

ADD AN AXIS

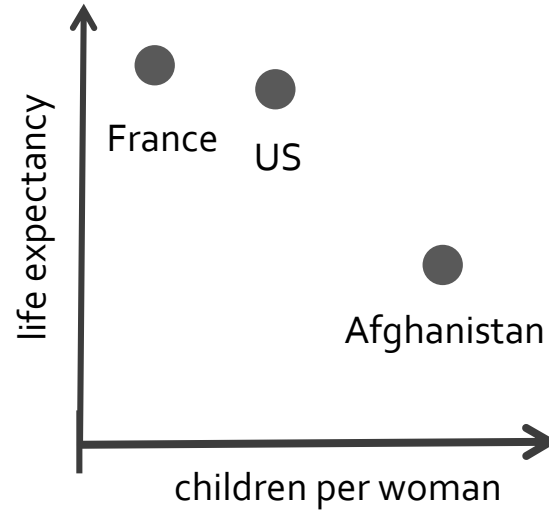
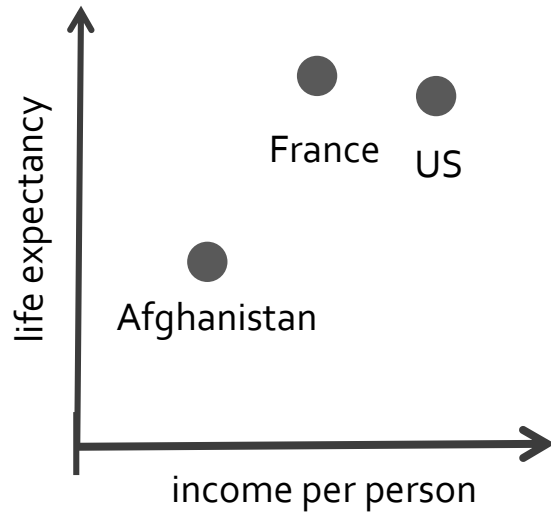


Problems:

Occlusion, perspective distortion, does not scale

→ Not usually recommended

ADD AN AXIS



SCATTERPLOT MATRIX

This idea scales relatively well

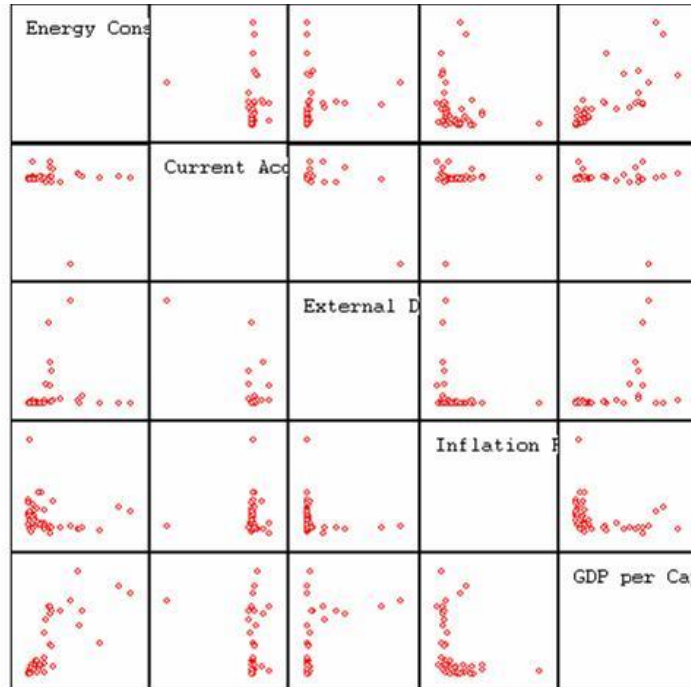


Image Source: Wikipedia

SCATTERPLOT MATRIX

movie IMDB ID

tt1430132

Load

The Wolverine

2013 - 2 h 6 min

Actors

Hugh Jackman (20)

Will Yun Lee (6)

Tao Okamoto (0)

Rila Fukushima (0)

Directors

James Mangold (6)

Writers

Mark Bombback (6)

Scott Frank (8)

Genres

Action (779)

Adventure (563)

Fantasy (366)

Sci-Fi (350)

Budgets

120000000 (238)

Producers

Hugh Jackman (2)

Tom Cohen (0)

Stan Lee (27)

Hutch Parker (1)

Costume_Designers

Composers

Marco Beltrami (40)

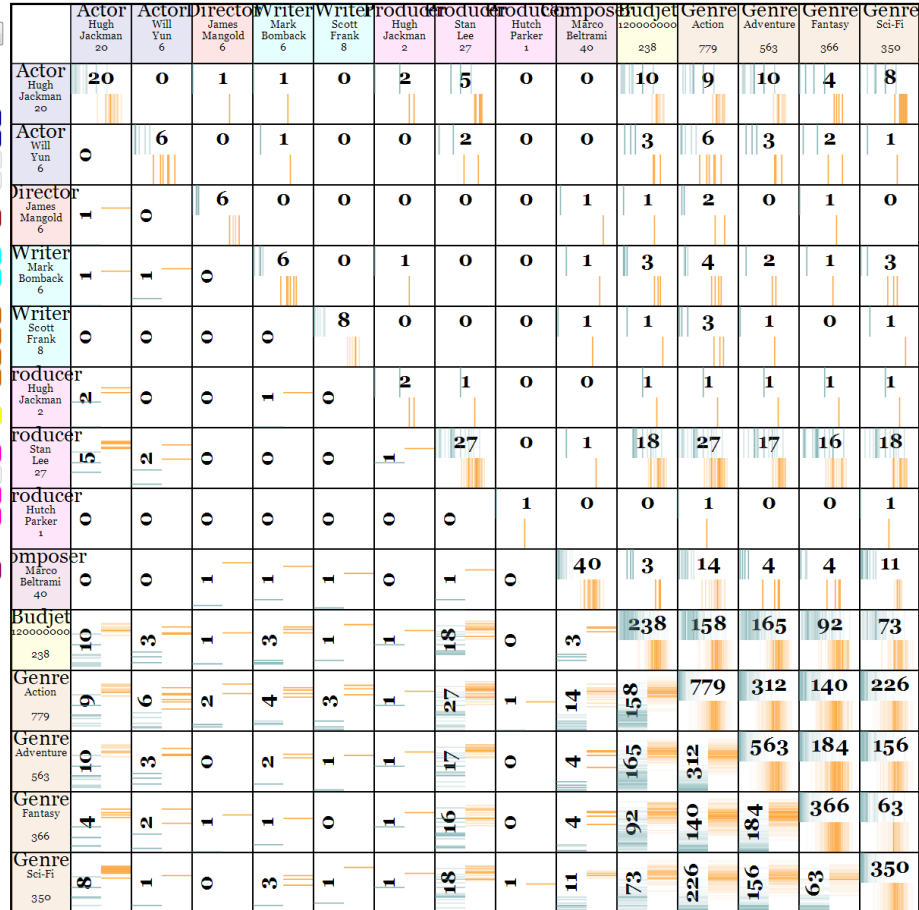
Cinematographers

Additional Informations

Composer

Marco Beltrami

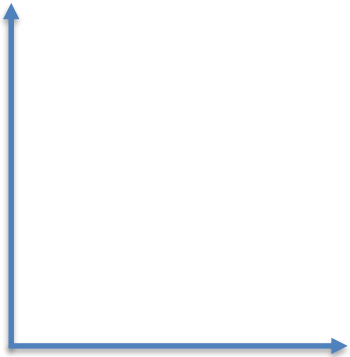
Add



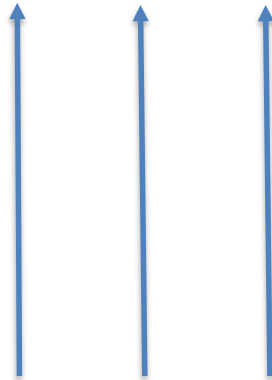
By Charles Perin

SPATIAL AXIS ORIENTATION

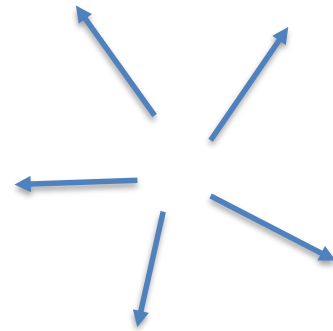
An additional design choice



rectilinear



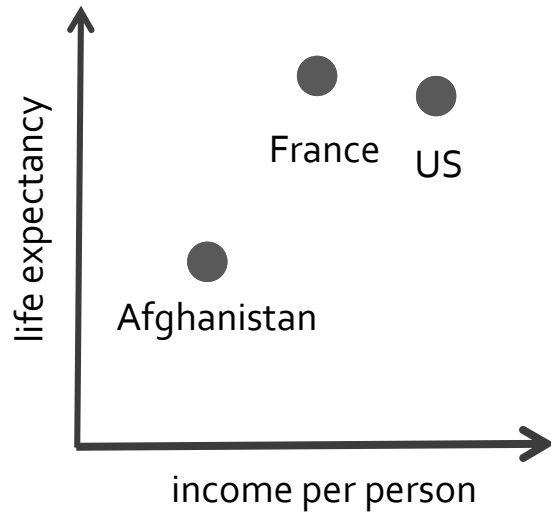
parallel



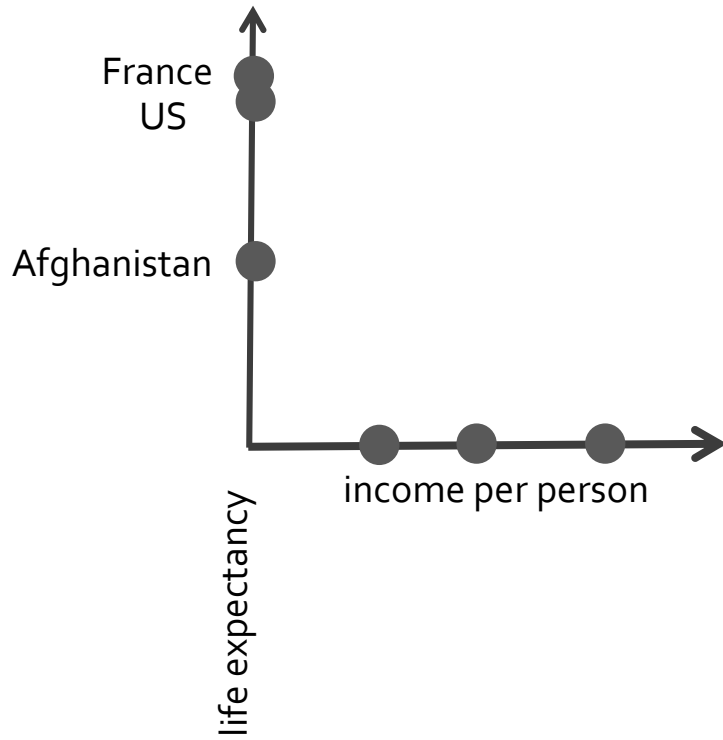
radial

parallel coordinates

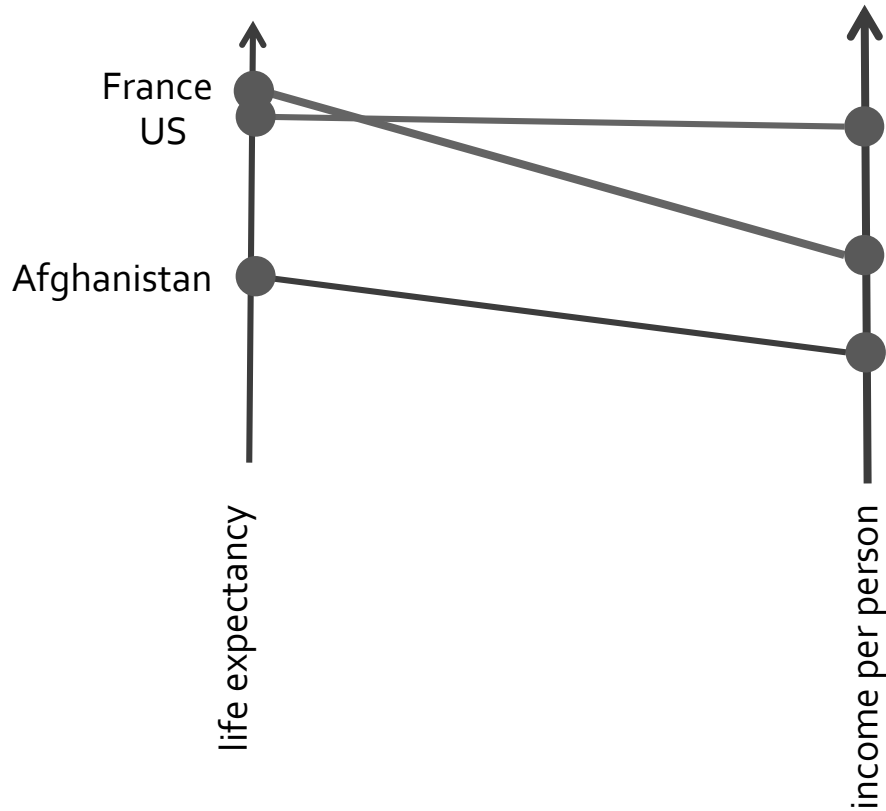
Back to our original example



Parallel Coordinates



parallel coordinates



- show correlations between neighboring axes

MULTIDIMENSIONAL DETECTIVE

Alfred Inselberg*, Multidimensional Graphs Ltd[†]
&
Computer Science Department
Tel Aviv University, Israel
aiisreal@math.tau.ac.il

Abstract

The display of multivariate datasets in parallel coordinates, transforms the search for *relations* among the variables into a 2-D pattern recognition problem. This is the basis for the application to *Visual Data Mining*. The Knowledge Discovery process together with some general guidelines are illustrated on a dataset from the production of a VLSI chip. The special strength of parallel coordinates is in modeling **relations**. As an example, a simplified Economic Model is constructed with data from various economic sectors of a real country. The visual model shows the interrelationship and dependencies between the sectors, circumstances where there is competition for the same resource, and feasible economic policies. Interactively, the model can be used to do trade-off analyses, discover sensitivities, do approximate optimization, monitor (as in a Process) and Decision Support.

Introduction

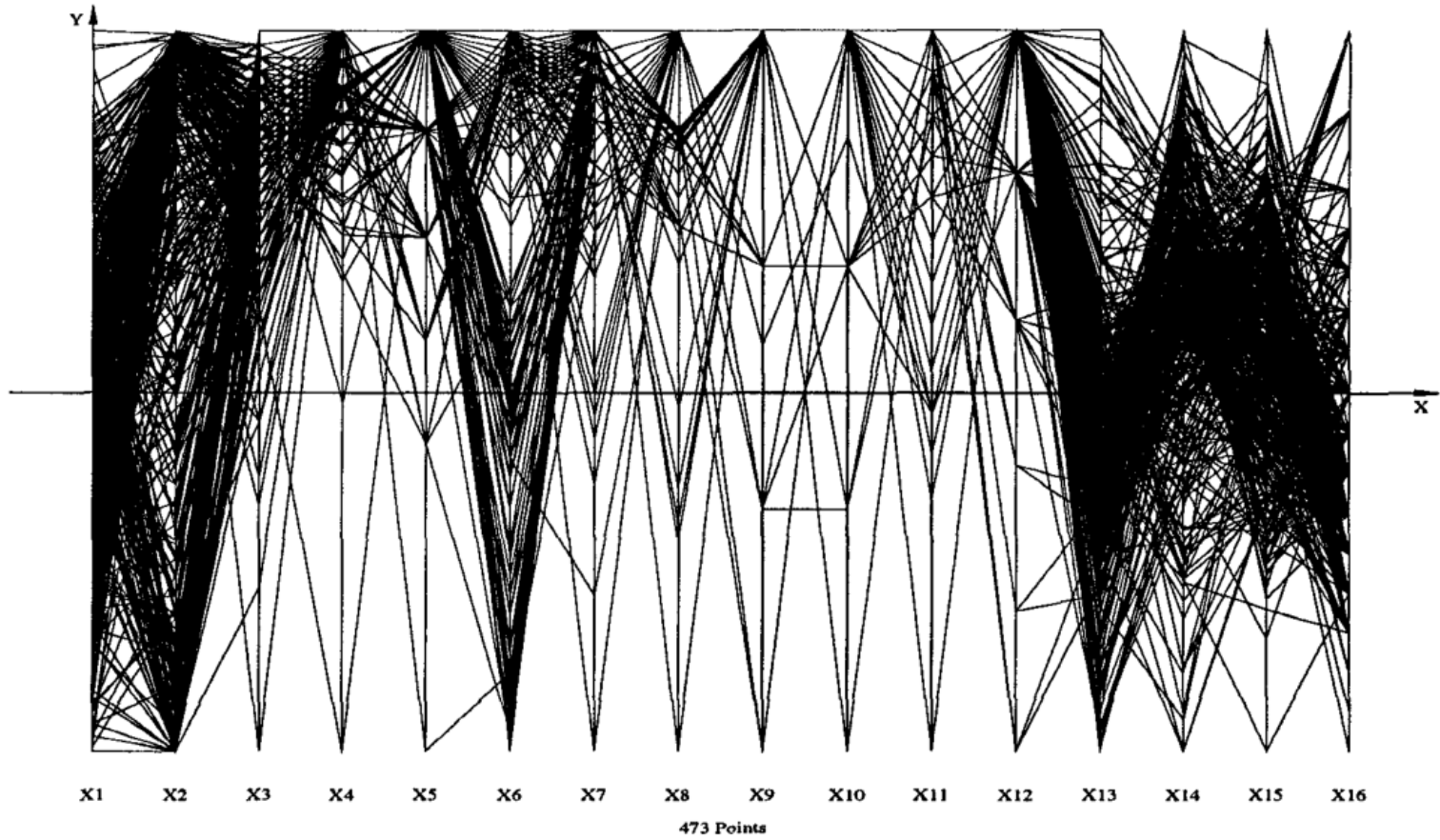
In Geometry parallelism, which does not require a notion of angle, rather than orthogonality is the more fundamental concept. This, together with the fact that orthogonality "uses-up" the plane very

fast, was the inspiration in 1959 for "Parallel" Coordinates. The systematic development began in 1977 [4]. The goals of the program were and still are (see [6] and [5] for short reviews) the visualization of multivariate/multidimensional problems without loss of information and having the properties:

1. Low representational complexity. Since the number of axes, N equals the number of dimensions (variables) the complexity is $O(N)$,
2. Works for any N ,
3. Every variable is treated uniformly (unlike "Chernoff Faces" and various types of "glyphs"),
4. The displayed object can be recognized under projective transformations (i.e. rotation, translation, scaling, perspective),
5. The display easily/intuitively conveys information on the properties of the N -dimensional object it represents,
6. The methodology is based on rigorous mathematical and algorithmic results.

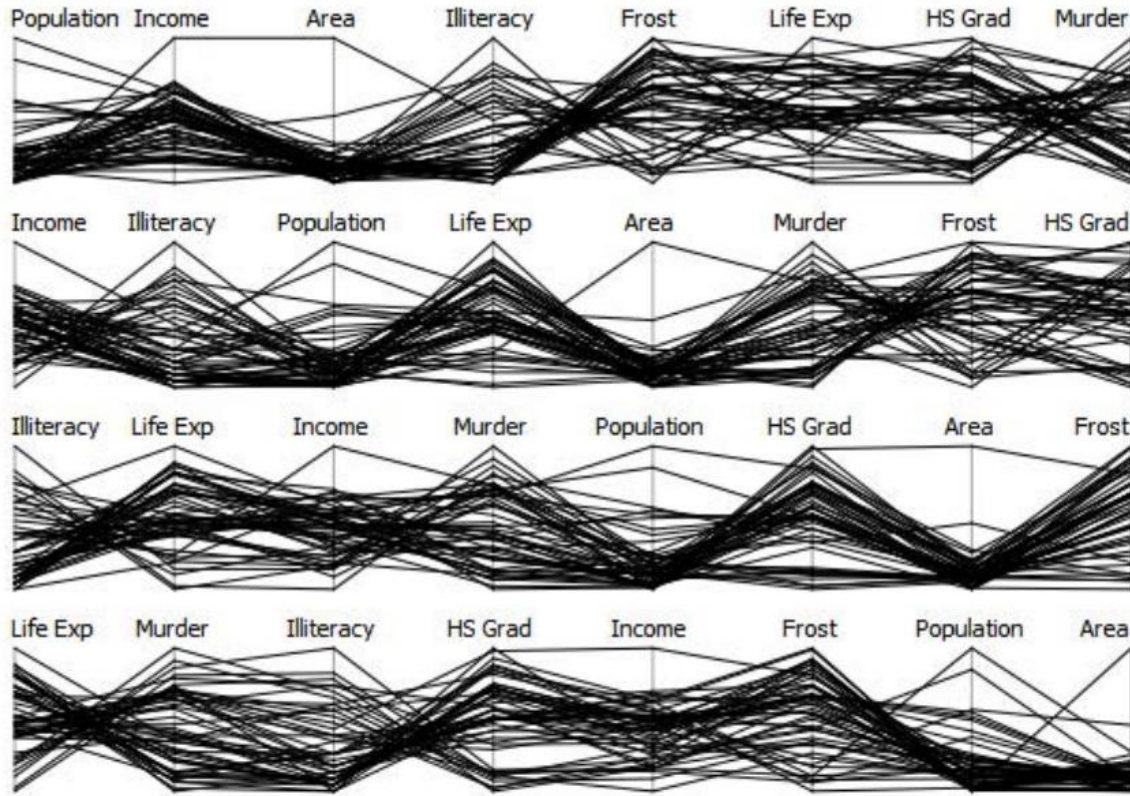
Parallel coordinates (abbr.||-coords) transform multivariate relations into 2-D patterns, a property that is well suited for Visual Data Mining.

* Senior Fellow San Diego SuperComputing Center
[†]36A Yehuda Halevy Street, Raanana 43556, Israel



Original Example from Inselberg 1997

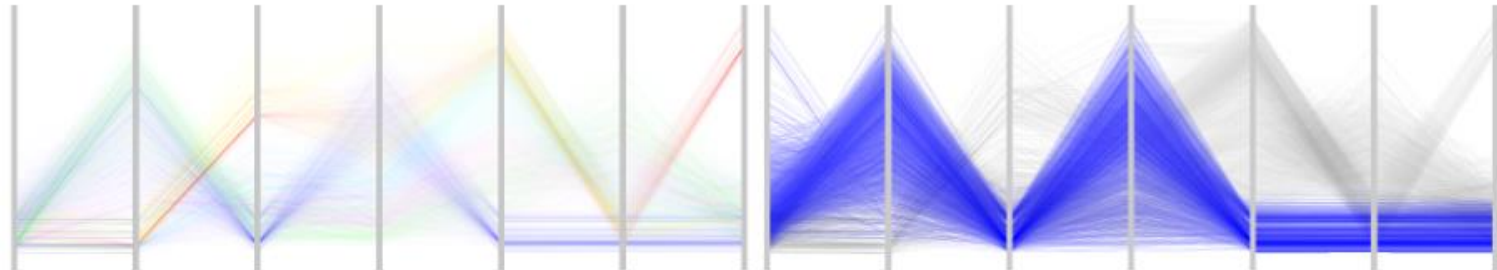
THE ORDER OF AXES MATTERS



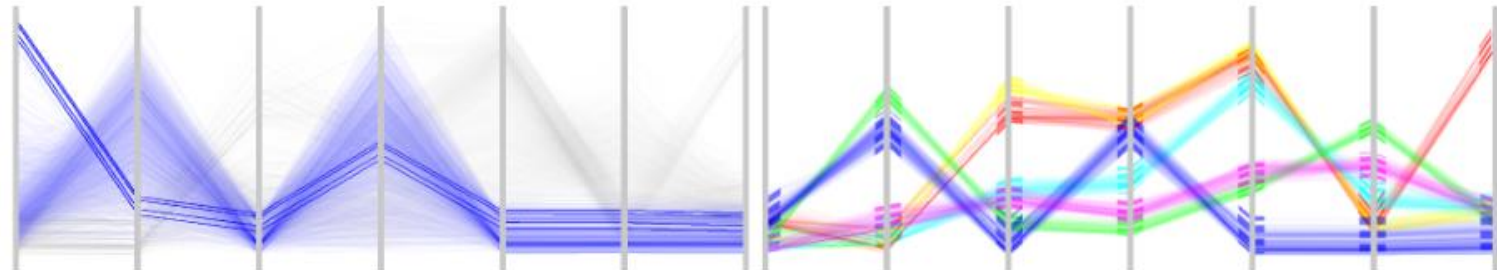
Eurographics 2013, STAR Report
J. Heinrich, D. Weiskopf

REDUCE CLUTTER - HIGHLIGHT CLUSTERS

Lots of work on this. For example:



(a) A linear transfer function has been applied to the high-precision texture in order to prevent cluttering and to provide overview of the data. (b) A logarithmic transfer function is applied to a selected cluster. The structure is preserved and emphasis is put on the low density regions.

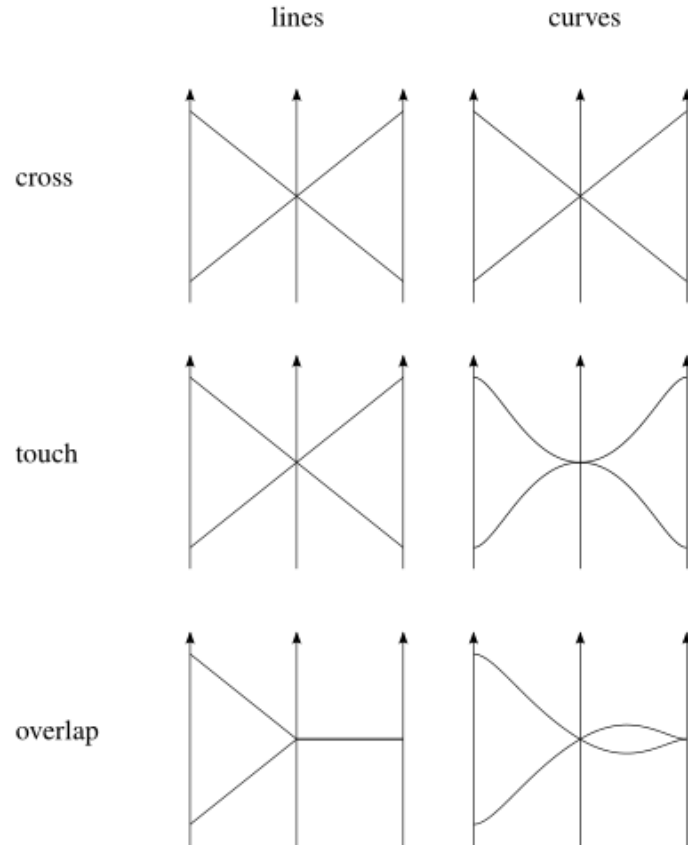


(c) Local cluster outliers are enhanced. A square root transfer function is used and the outliers are visible even through high-density regions. (d) A complementary view of the clusters with uniform bands. 'Feature animation' presents statistics about the clusters and acts as a guidance.

Revealing Structure within Clustered Parallel Coordinates Displays, InfoVis 2005

HOW TO DRAW THE LINES

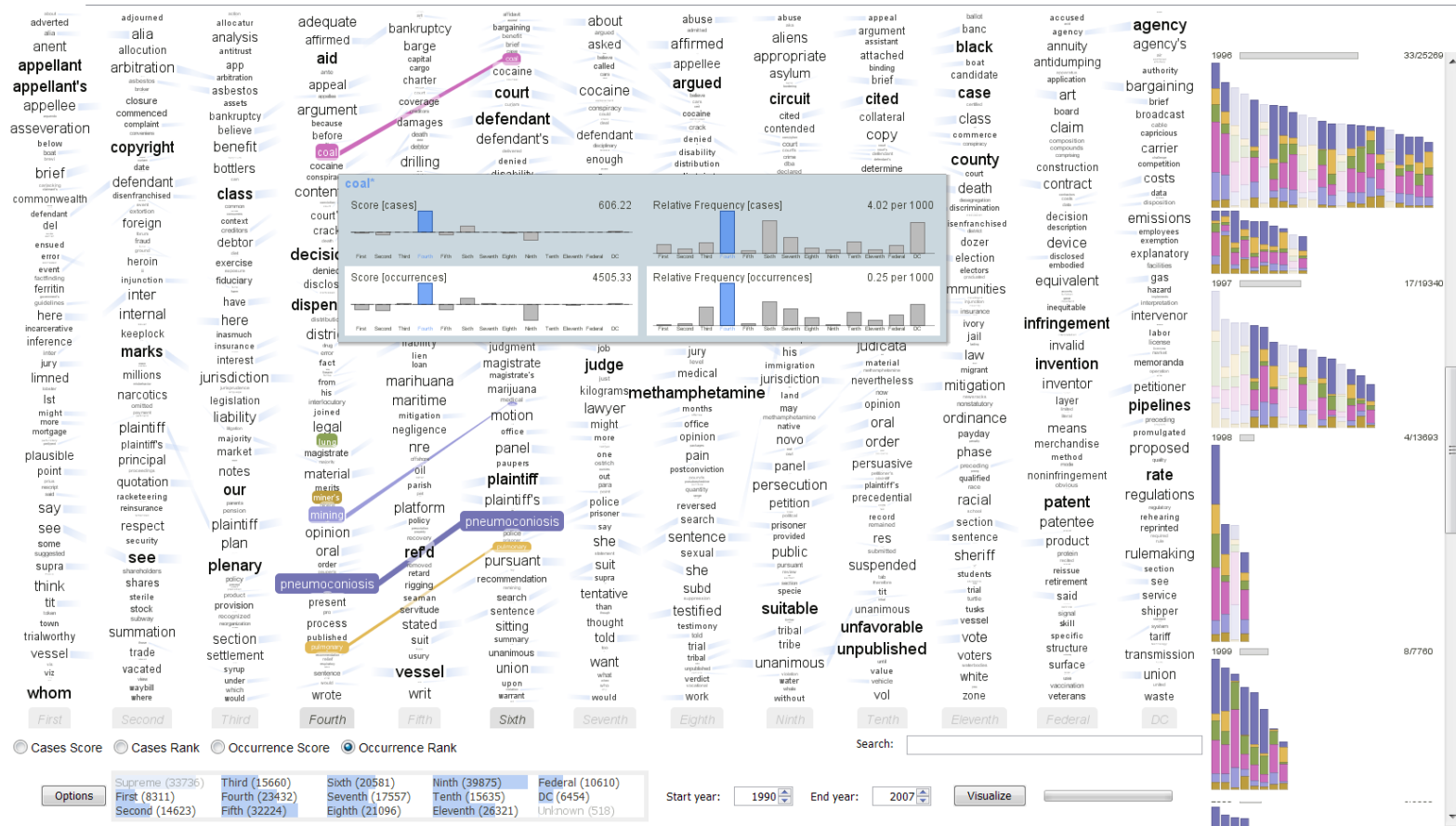
Goal: avoid ambiguity



Eurographics 2013, STAR Report
J. Heinrich, D. Weiskopf

COMBINE WITH OTHER VISUALIZATION TECHNIQUES

Parallel Tag Clouds to Explore Faceted Text Corpora (Collins et al., VAST 2009)



THERE IS MUCH MORE ON THIS...

Start here if you want more information

EUROGRAPHICS 2013/ M. Sbert, L. Szirmay-Kalos

STAR – State of The Art Report

State of the Art of Parallel Coordinates

J. Heinrich and D. Weiskopf

Visualization Research Center, University of Stuttgart

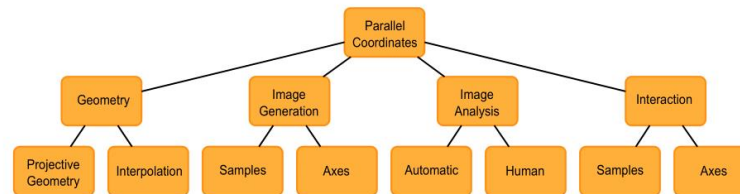


Figure 1: Taxonomy of topics for parallel coordinates in the scientific literature. The first-level nodes each represent a section in this paper, where the scope and definition of each topic will be explained.

Abstract

This work presents a survey of the current state of the art of visualization techniques for parallel coordinates. It covers geometric models for constructing parallel coordinates and reviews methods for creating and understanding visual representations of parallel coordinates. The classification of these methods is based on a taxonomy that was established from the literature and is aimed at guiding researchers to find existing techniques and identifying white spots that require further research. The techniques covered in this survey are further related to an established taxonomy of knowledge-discovery tasks to support users of parallel coordinates in choosing a technique for their problem at hand. Finally, we discuss the challenges in constructing and understanding parallel-coordinates plots and provide some examples from different application domains.

Categories and Subject Descriptors (according to ACM CCS): I.3.3 [Computer Graphics]: Picture/Image Generation—Line and curve generation

Scattering Points in Parallel Coordinates

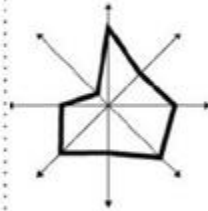
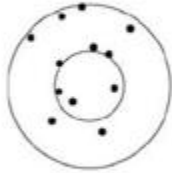
Xiaoru Yuan,¹ Peihong Guo,¹ He Xiao,¹ Hong Zhou,² Huamin Qu²

1. Key Laboratory of Machine Perception (MOE), School of EECS, Peking University

2. Department of Computer Science and Engineering at Hong Kong University of Science and Technology,
Clear Water Bay, Kowloon, Hong Kong

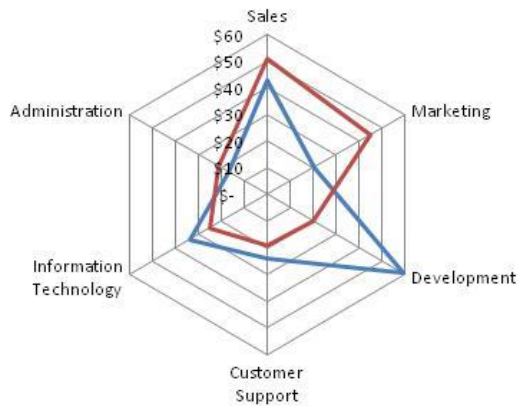
RADIAL AXES

Polar

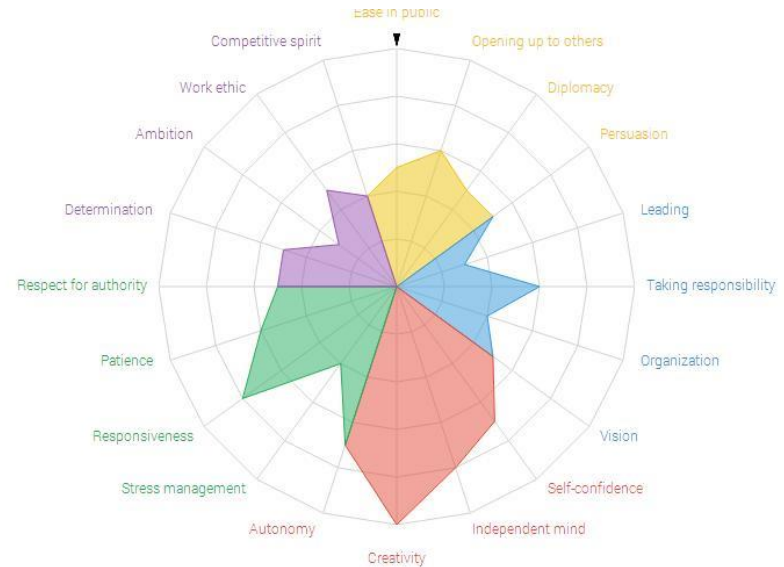


EXAMPLE: STAR PLOT

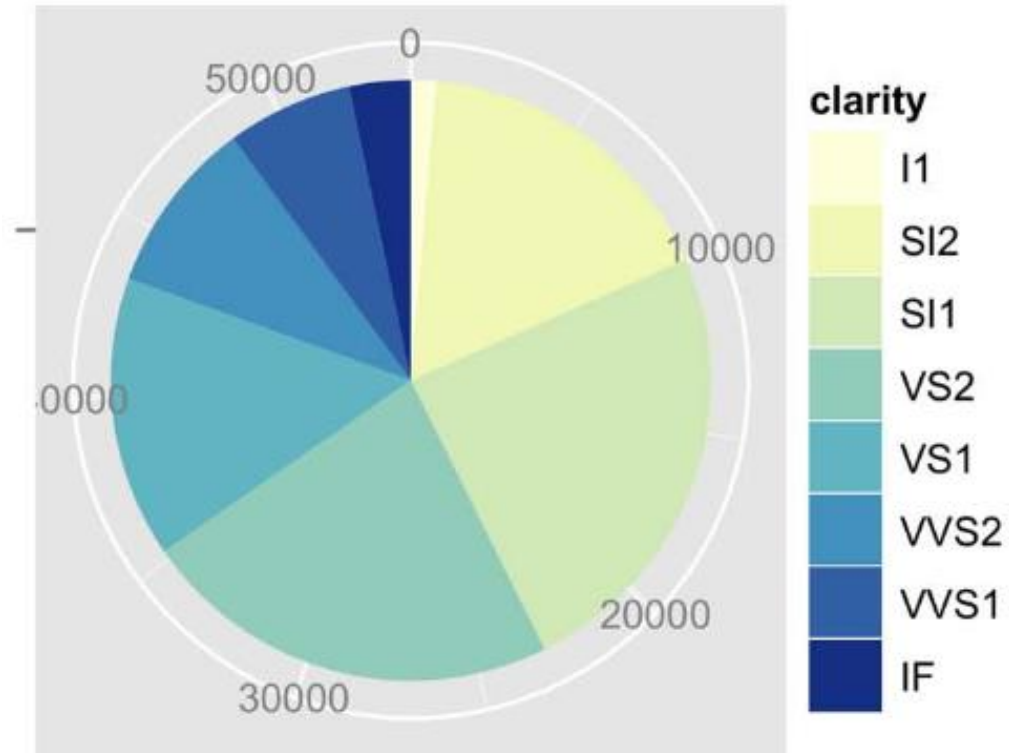
- = radial line chart



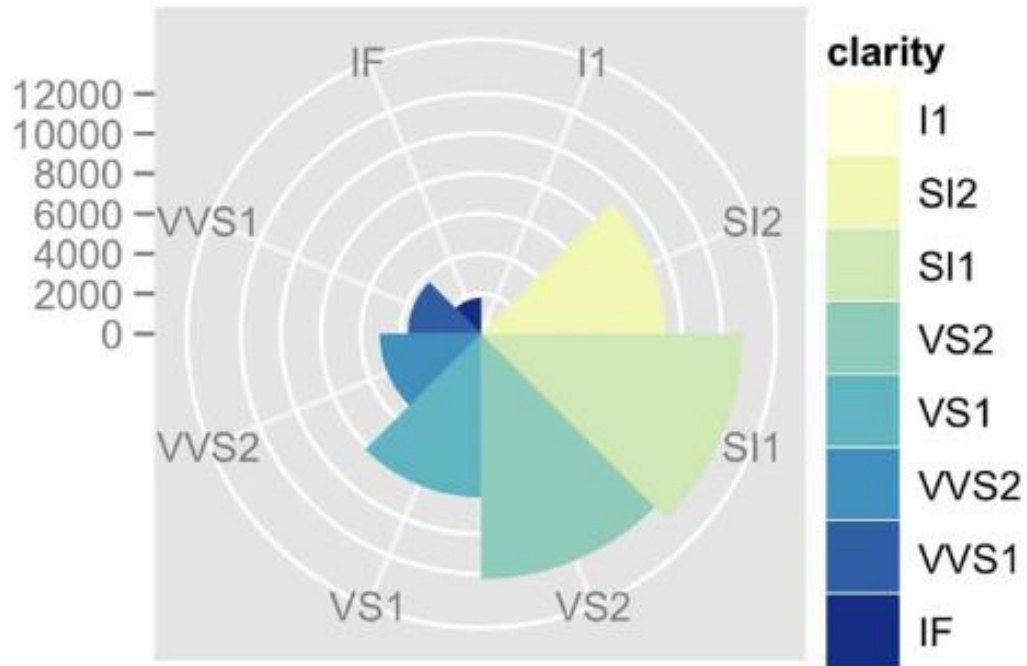
— Allocated Budget
— Actual Spending



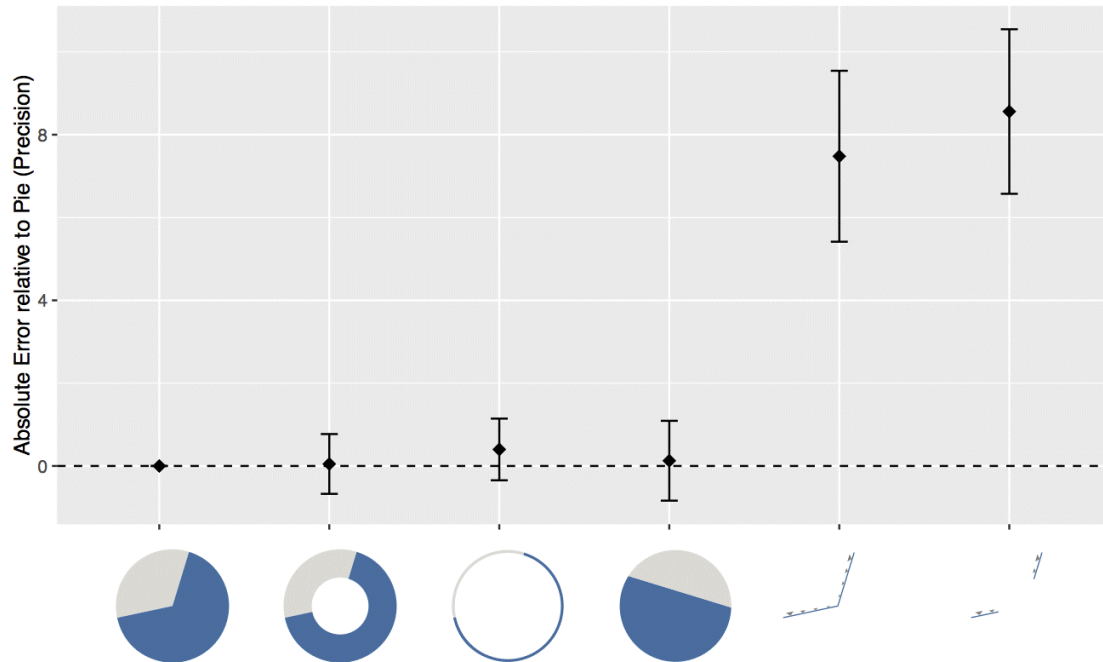
PIE CHARTS



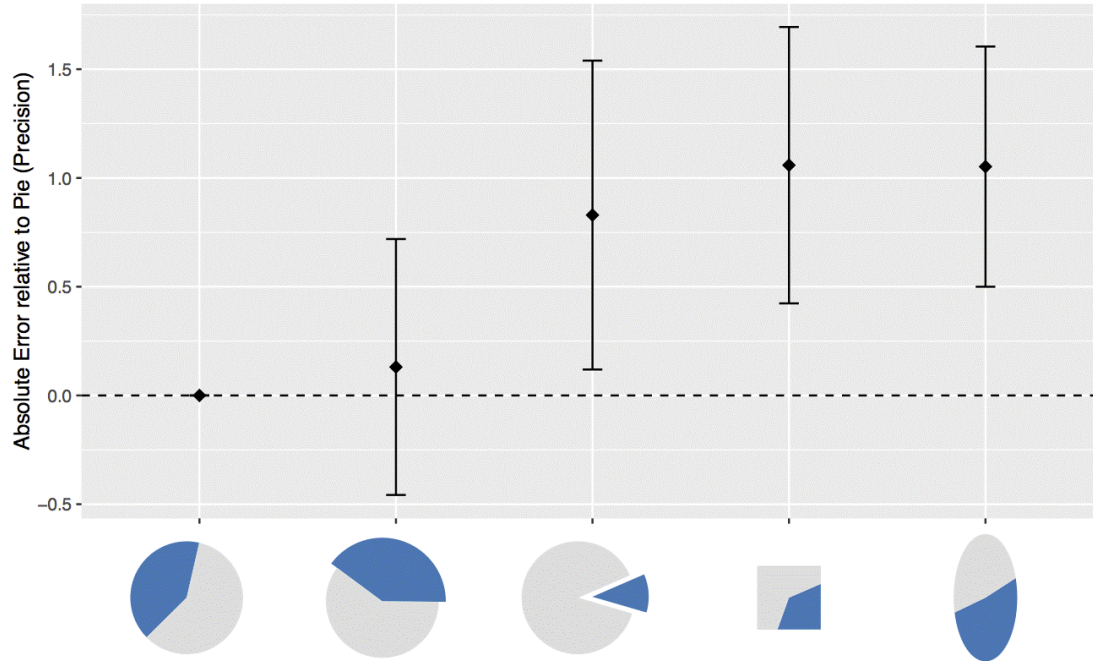
POLAR AREA CHARTS



HOW DO PEOPLE READ PIE CHARTS?



HOW DO PEOPLE READ PIE CHARTS?



SPATIAL LAYOUT DENSITY

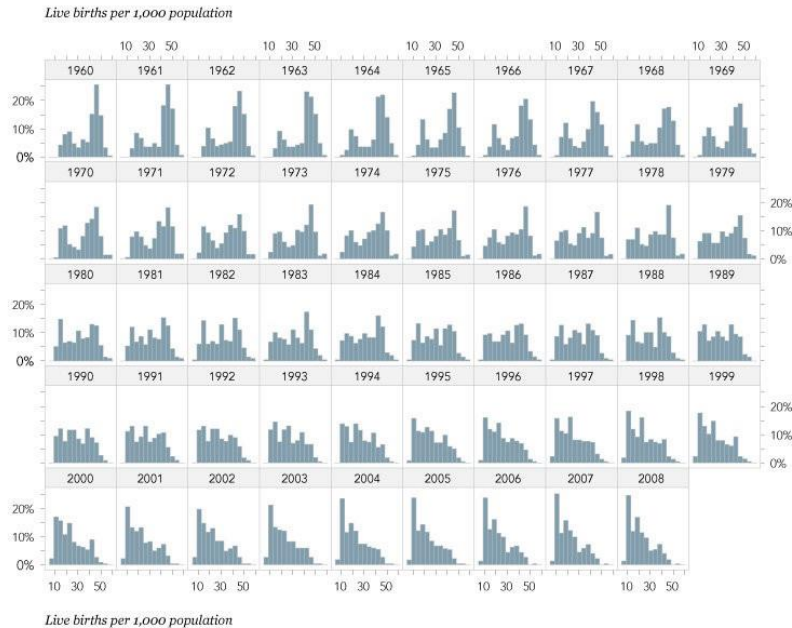
DATA DENSITY

MAXIMIZE THE RATIO OF:

$$\frac{\text{(NUMBER OF ENTRIES IN DATA)}}{\text{(AREA OF THE GRAPHIC)}}$$

DATA DENSITY – SHRINK THE GRAPHICS

Annual Worldwide Distributions of Live Births



“SMALL MULTIPLES”

DATA DENSITY – SHRINK THE GRAPHICS

GRAPHIC PROBLEMS POSED BY TIME SERIES

Scale in years

With a scale in years, a two-year total (figure 1) should be divided by 2 (figure 2). A total for six months should be multiplied by 2.

Pointed curves

For overly pointed curves (figure 3), the scale of the Q should be reduced; optimum angular perceptibility occurs at around 70 degrees (figure 4).

If the curve is not reducible (large and small variations), filled columns can be used (figure 5).

Flat curves

For overly flat curves (figure 6), the scale of the Q should be increased (figure 7).

Small variations

For small variations in relation to the total (figure 8), the total loses its importance, and the zero point can be eliminated (figure 9). The graphic can be interpreted as an acceleration if a precise study of the variations is necessary; here, we use a logarithmic scale (figure 10). (See also page 240.)

Large range

For a very large range between the extreme numbers (figure 11), we must either:

- (1) leave out the smallest variations;
- (2) be concerned only with relative differences (logarithmic scale), without knowing the absolute quantities;
- (3) select different parts (periods) within the ordered component and treat them on different scales above the common scale (figure 12).

Obvious periodicity

If there is obvious periodicity (figure 13), and the study involves a comparison of the phases of each cycle, it is preferable to break up the cycles in order to superimpose them (figure 14). A polar construction can be used, preferably in a spiral shape (figure 15), but we should not begin with too small a cycle. As striking as it seems, it is less efficient than an orthogonal construction.

Annual curves

For annual curves of rainfall or temperature, if a cycle has two phases (figure 17), why depict only one (figure 16)?

A contrast

Unlike what we see in figure 18, the pertinent or "new" information must be separated from the background or "reference" information. The background involves: (a) the invariant, highlighted by a heading (Port St. Michel); (b) the highly visible identification of each component (image and date). The new information (the curve) must stand out from the background (figure 19).

Reference points

It is impossible to utilize a graphic such as figure 20, except in a general manner. There is confusion concerning the position of the points, and no potential comparison is possible, as it is in figure 21.

Precision reading

A precision reading (utilization on the elementary level, as in figure 24) is difficult in figure 22, which results in a poor reading of the order of the points, and in figure 23, where there is ambiguity concerning the position of the points. On the other hand, figure 22 does favor overall vision (correlation).

Null boxes

Curves accommodate null boxes poorly (figure 25). Columns (figure 26) are preferable.

Unknown boxes

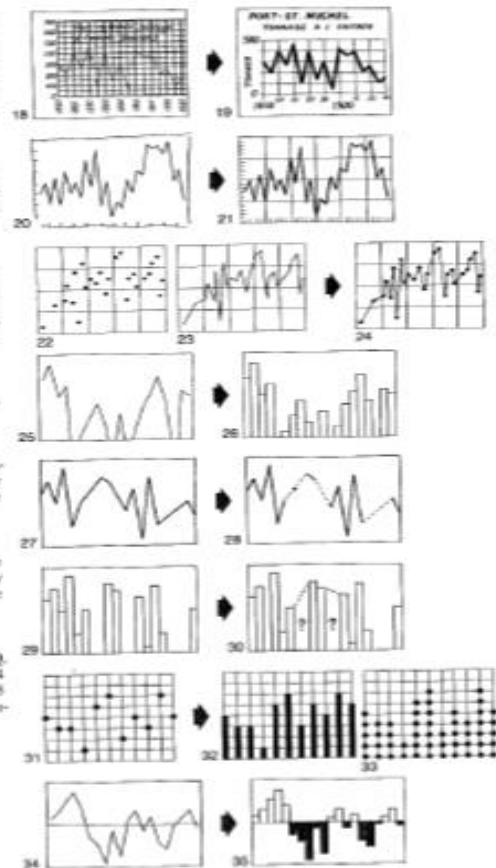
The drawing must indicate the unknowns of the information in an unambiguous way (figures 28 and 30). The reader might interpret figure 27 as a change in the structure of the curve and figure 29 as involving null values.

Very small quantities

Except in seeking a correlation (quite improbable here) the number of ships entering into a port is represented better by figure 33 than by figures 31 or 32. The reader can perceive the numerical values at first glance.

Positive-negative variation

This is in fact a problem involving three components O, Q, \neq (+, -), and it must be visually treated as such. Figure 34 can be improved by utilizing a setial variable (in figure 35 a value difference: black-white) to differentiate the \neq component and thus highlight positive-negative variation.



DATA DENSITY – SHRINK THE GRAPHICS

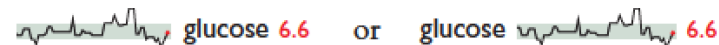
Placed in the relevant context, a single number gains meaning. Thus the most recent measurement of glucose should be compared with earlier measurements for the patient. This data-line shows the path of the last 80 readings of glucose:



Lacking a scale of measurement, this free-floating line is dequantified. At least we do know the value of the line's right-most data point, which corresponds to the most recent value of glucose, the number recorded at far right. Both representations of the most recent reading are tied together with a color accent:



Some useful context is provided by showing the *normal range* of glucose, here as a gray band. Compared to normal limits, readings above the band horizon are elevated, those below reduced:



SPARKLINES

Science fiction

From Wikipedia, the free encyclopedia

For other uses, see [Science fiction \(disambiguation\)](#).

33k visits in last 30 days

Science fiction is a genre of [fiction](#) dealing with imaginative content such as [futuristic](#) settings, futuristic [science](#) and [technology](#), [space travel](#), [time travel](#), [parallel universes](#), and [extraterrestrial life](#). It often explores the potential consequences

SPARKLINES

EASTERN EUROPE

Soviet cult and pragmatism in Transnistria

Experts worry that the next "Crimea" could be the breakaway region of Transnistria

Many locals there don't share that fear, and if the last referendum holds, a large majority would welcome a Russian annexation.



SPARKLINES

Gonzalo Higuaín slides
a cross in from the right



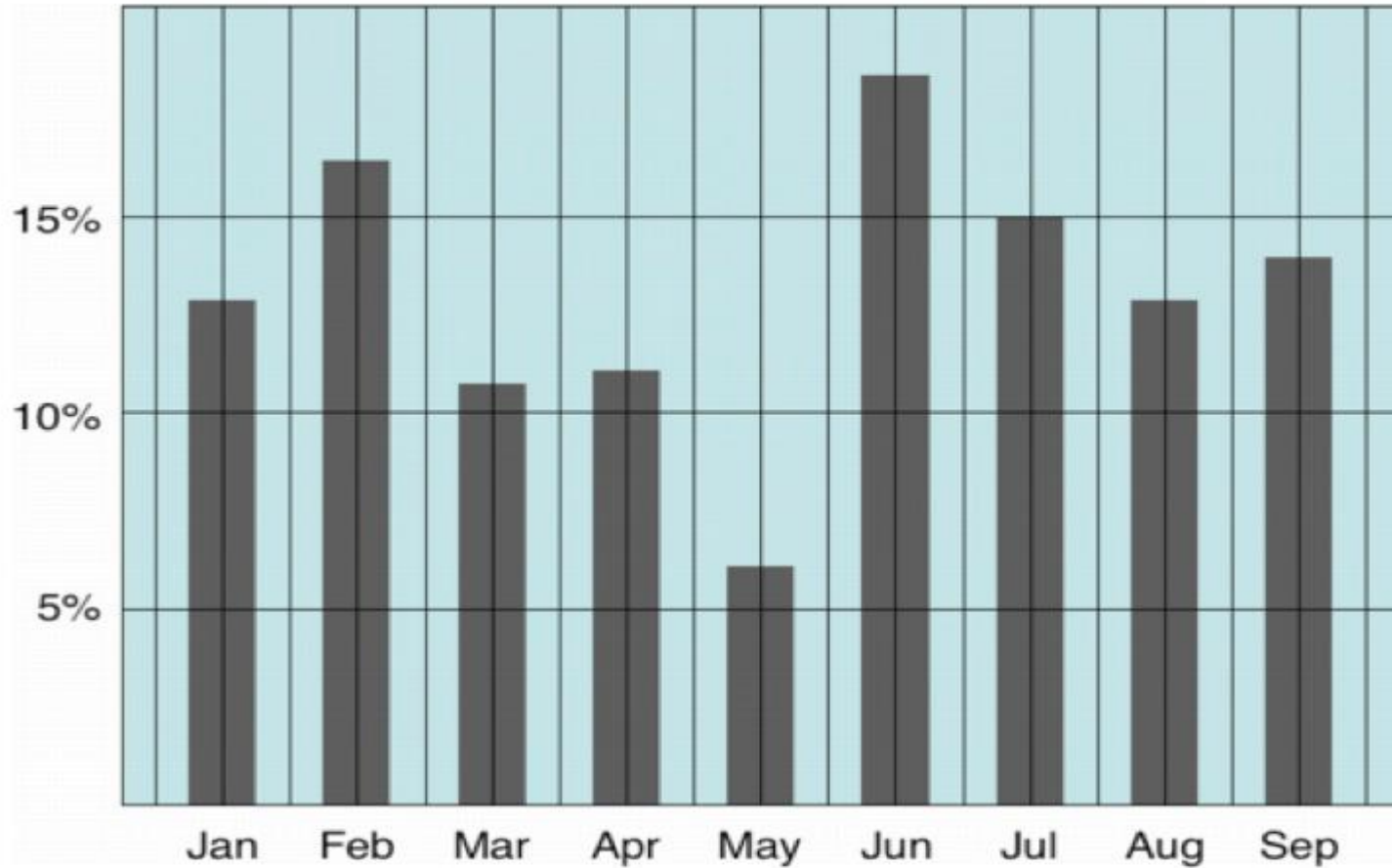
and Ronaldo,
at the front post, shoots
off target.

DATA-INK RATIO

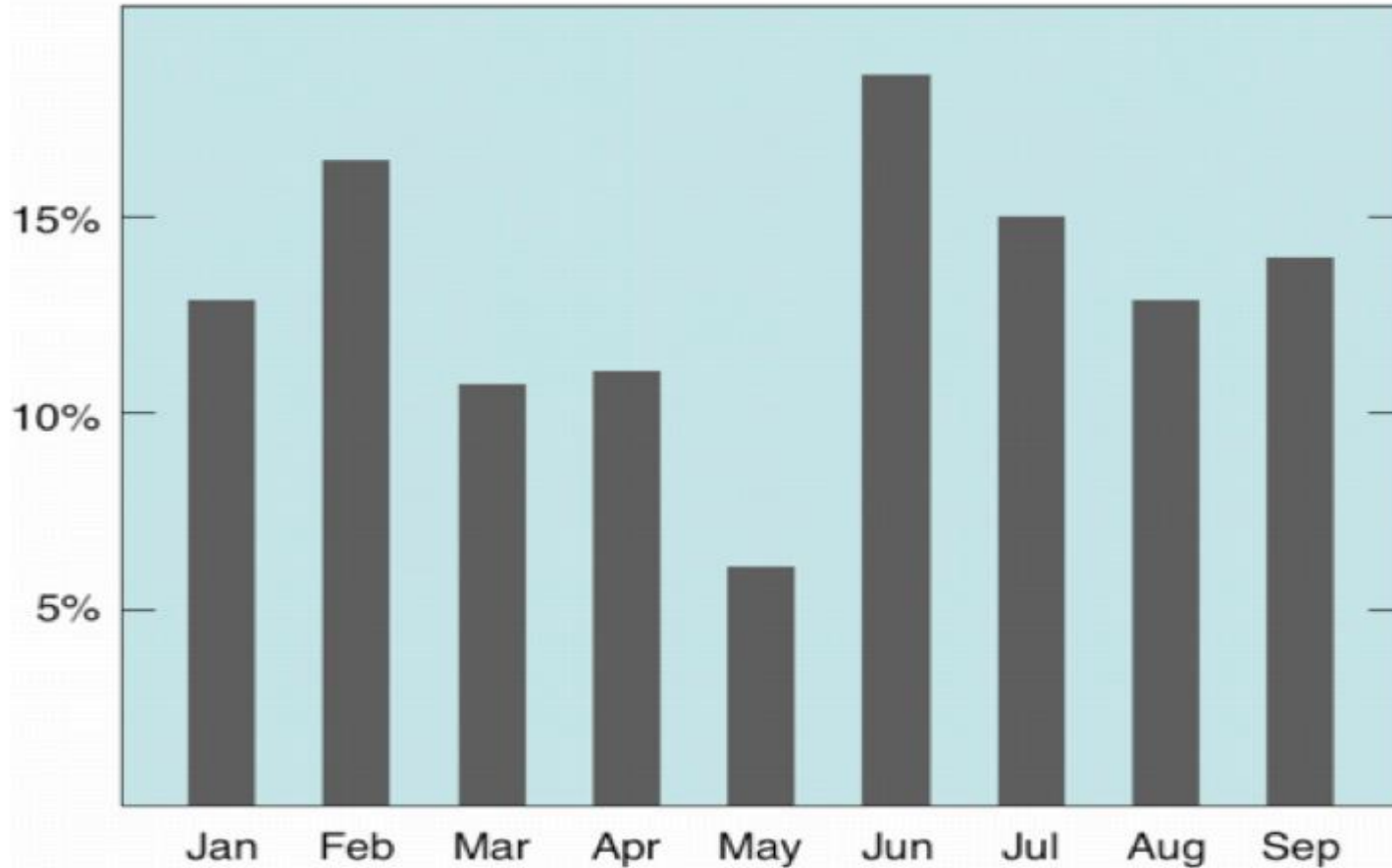
MAXIMIZE THE RATIO OF

$$\frac{\text{(INK USED TO SHOW DATA)}}{\text{(TOTAL INK USED)}}$$

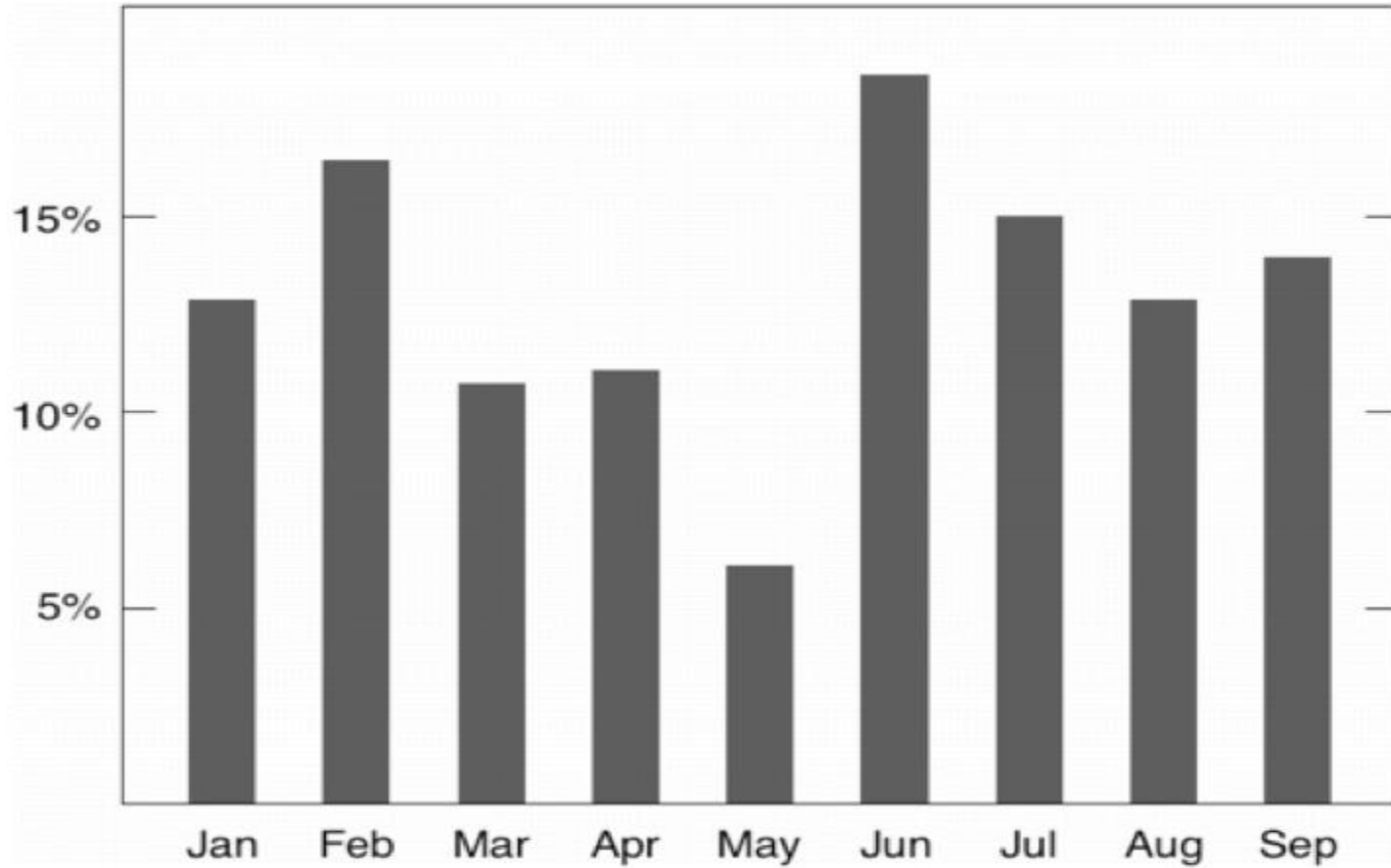
DATA-INK RATIO



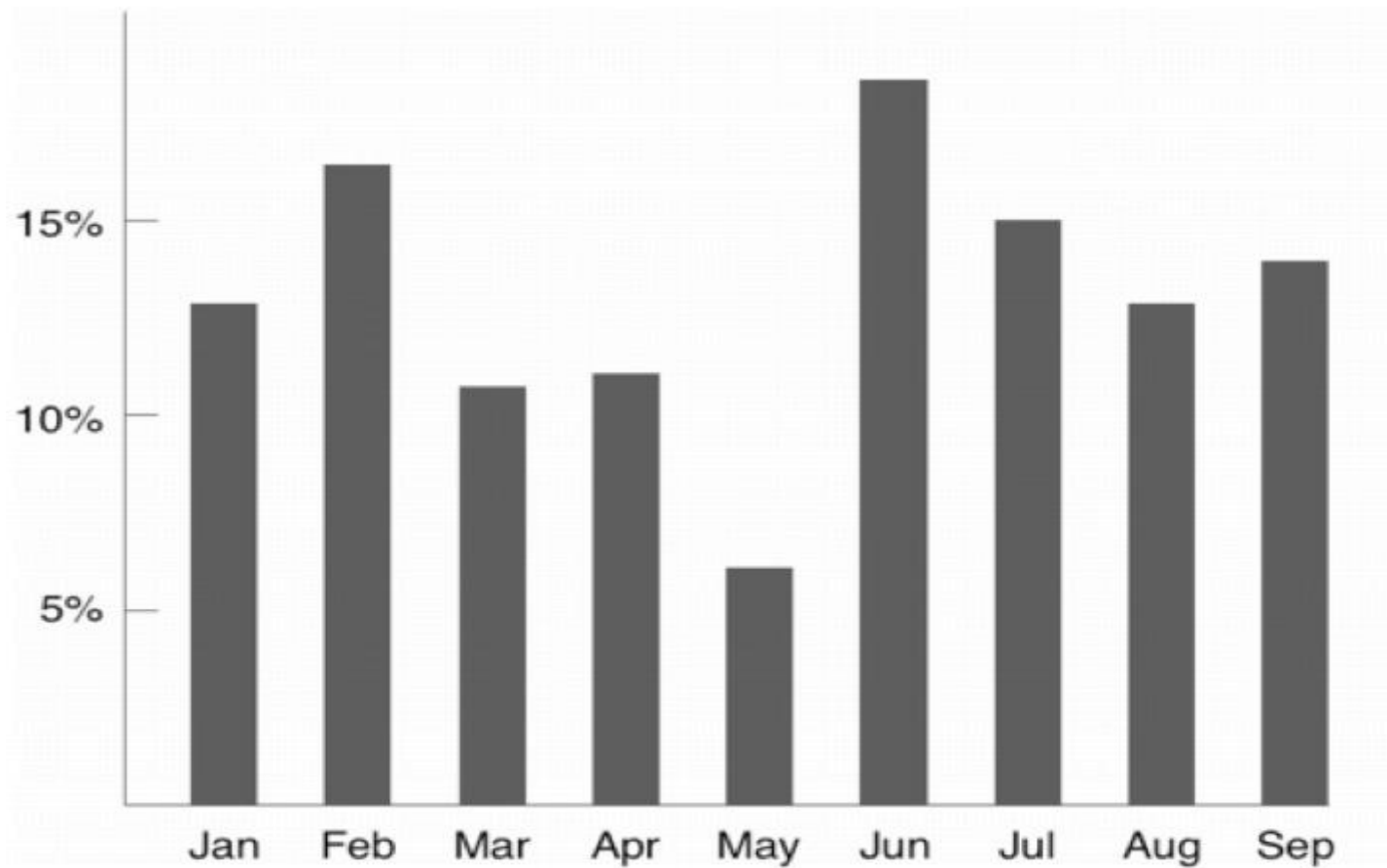
DATA-INK RATIO



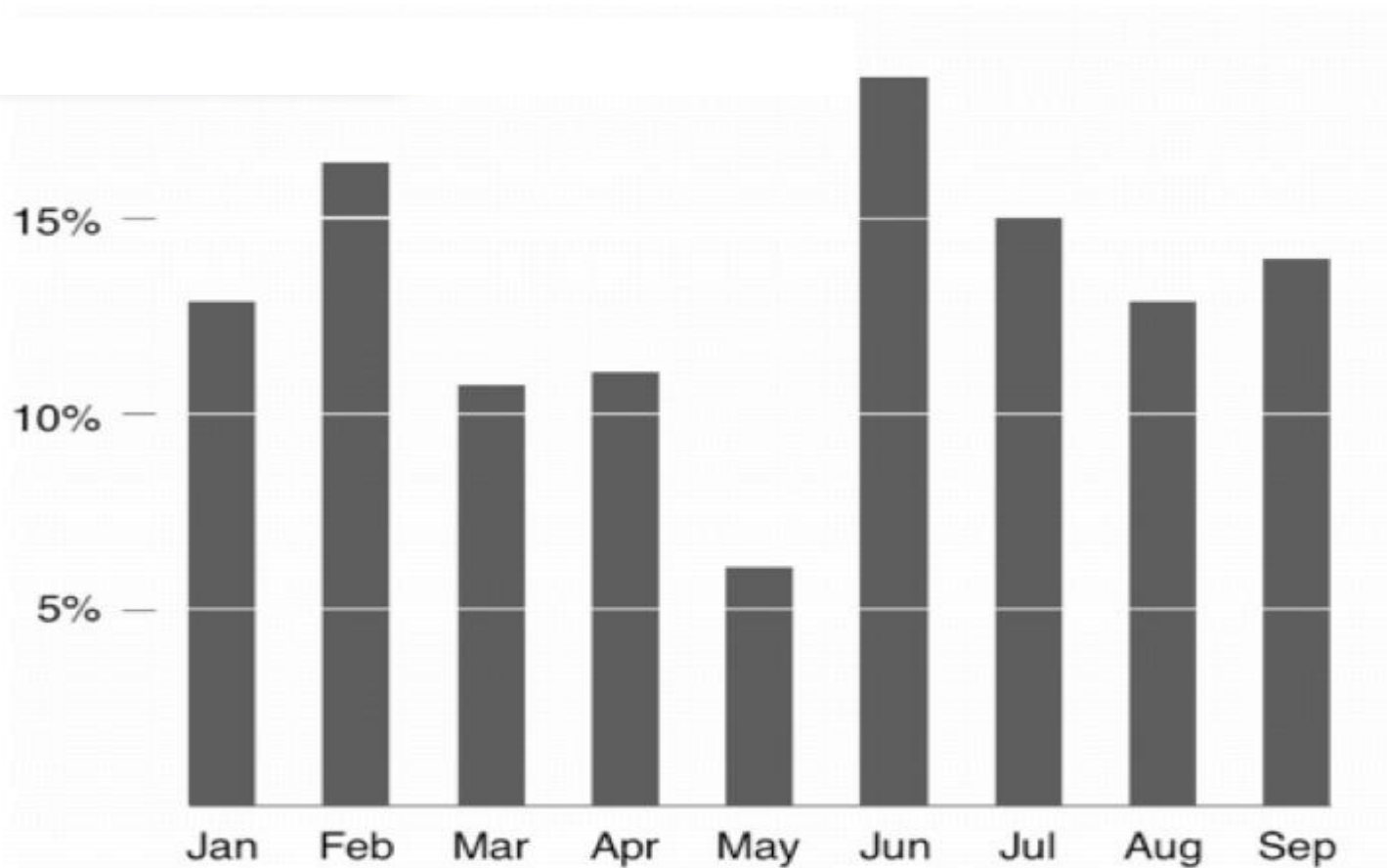
DATA-INK RATIO



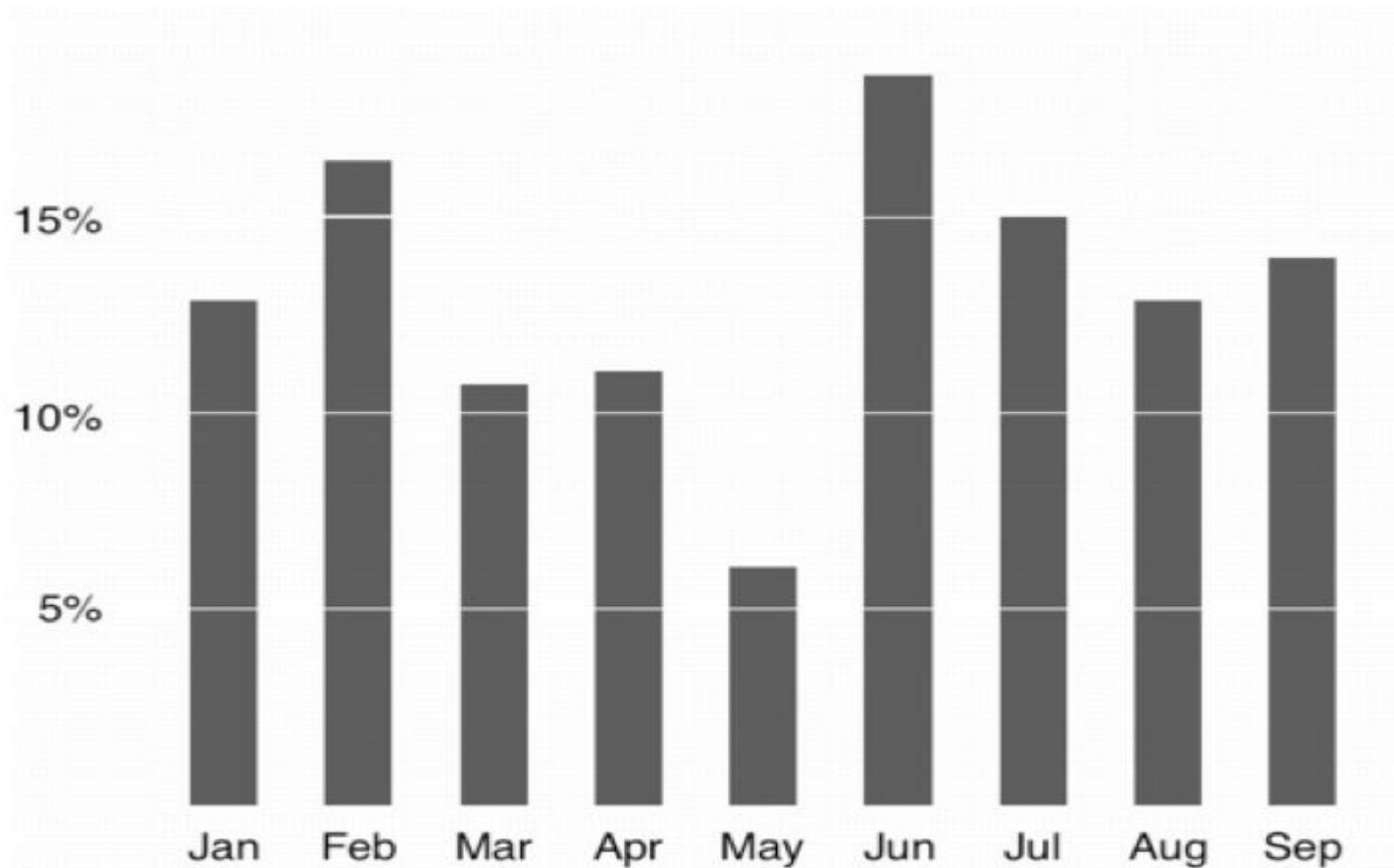
DATA-INK RATIO



DATA-INK RATIO



DATA-INK RATIO



MINIMIZE CHART JUNK

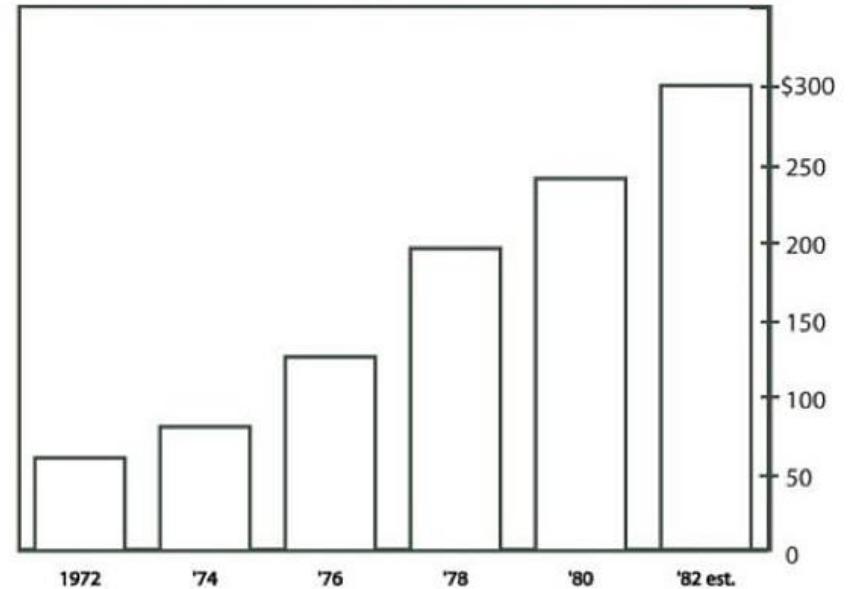
MONSTROUS COSTS

Total House and Senate campaign expenditures, in millions



MONSTROUS COSTS

Total House and Senate campaign expenditures, in millions



Wayne Lytle

The Dangers of
GLITZINESS
and other
Visualization Faux Pas

or... "What's Wrong with this Visualization?"

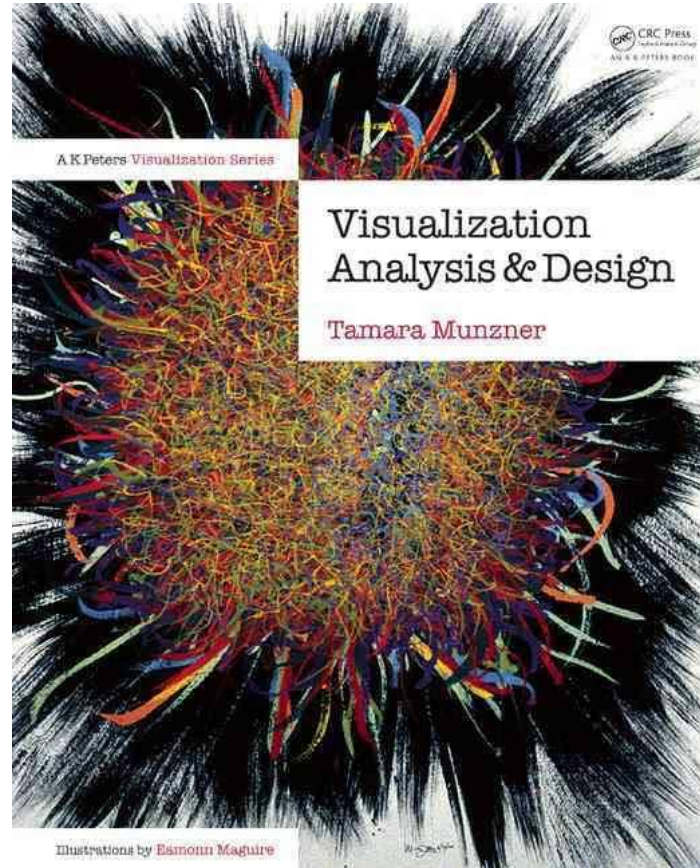
TUFTE'S INTEGRITY PRINCIPLES

- MAXIMIZE THE DATA-INK RATIO
- AVOID CHART JUNK (*SOMETIMES*)
- LAYER INFORMATION
- MAXIMIZE THE DATA DENSITY
 - *SHRINK THE GRAPHICS*
 - *MAXIMIZE THE AMOUNT OF DATA SHOWN (SOMETIMES)*



EDWARD TUFTE

READINGS



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- Saul Greenberg (University of Calgary)